

Corrections/amendments to **Dynamic Models for Volatility and Heavy Tails**

p 12. 3 lines up from (1.16)  $\varphi_{t+1|t} = (\nu - 2)^{1/2}\sigma_{t+1|t}$  should be  $\varphi_{t+1|t} = ((\nu - 2)/\nu)^{1/2}\sigma_{t+1|t}$ .

p 22 last line of sub-section 2.1.2 ‘The kurtosis is  $\Gamma(5/\nu)\Gamma(1/\nu)$ , so for  $\nu = 1$  the excess kurtosis is nine.’ should be

‘The kurtosis is  $\Gamma(5/\nu)\Gamma(1/\nu)/(\Gamma(1/\nu))^2$ , so for  $\nu = 1$  the excess kurtosis is three.’

p 27 The off-diagonal elements in the information matrix at the top of the page should be multiplied by *minus* 2. Similarly the information matrix in (2.18) should read

$$\mathbf{I} \begin{pmatrix} \mu \\ \lambda \\ \nu \end{pmatrix} = \begin{bmatrix} \frac{\nu+1}{\nu+3} \exp(-2\lambda) & 0 & 0 \\ 0 & \frac{2\nu}{\nu+3} & \frac{-2}{(\nu+3)(\nu+1)} \\ 0 & \frac{-2}{(\nu+3)(\nu+1)} & h(\nu)/2 \end{bmatrix}, \quad (2.18)$$

The same correction should be made on pages 65 and 116.

With the change in (2.18), the entries for  $\lambda$  and  $\nu$  in Tables 3.1 and 3.2 change ( see below)

p 28 The entry for  $\mu$  in the information matrix is incorrect. Rather than  $(\nu/2)^2 \exp(-2\lambda\nu)$  it should be

$$\nu^2 2^{-1/\nu} \exp(-2\lambda) \Gamma(2 - 1/\nu) / \Gamma(1/\nu)$$

NB. For  $\nu = 1$  it is  $(1/4) \exp(-2\lambda)$  whereas for  $\nu = 2$  it becomes  $\exp(-2\lambda)$ .

p 37 line 4 should not have absolute values, ie  $[E|x_t|)]^2$  should be  $[E(x_t)]^2$ .

p 41 The condition  $|a| < 1$  in Lemmas 9 and 10 is not sufficient. The error comes from incorrectly writing  $|a| = |E(x_t)|$  as  $|a| = E(|x_t|)$ . It should be replaced by  $b < 1$ . Since  $b = E(x_t^2) = E(|x_t|^2) \geq [E(|x_t|)]^2$ , it follows that  $b < 1$  is sufficient to ensure that  $E(|x_t|) < 1$  and this in turn ensures that  $E(\ln |x_t|) < 0$  by Jensen’s inequality.

p 43 6 lines from bottom, after *IID* delete ‘with zero location and unit scale’

p 46-7 Lemma 10 and Corollary 9 are modified as in the note on Lemma 10.

p 68-9 Tables 3.1 and 3.2. The ASEs need to be amended as discussed in the Note on Lemma 10

p 89 In (3.63) each  $\partial f$  should be  $\partial \ln f$

p 119 . The ASEs in tables 4.1, 4.4, 4.7 and 4.8 need to be re-calculated as in the Note on Lemma 10.

p 165 The expression

$$E \left[ u_t \frac{\partial u_t}{\partial \lambda} \right] = \frac{\nu^3 \xi \varsigma (\xi + \varsigma) (\xi + 1)}{(\varsigma + \xi + 2)(\varsigma + \xi + 1)} - \frac{\nu^3 \xi \varsigma}{(\xi + \varsigma + 1)}$$

should be

$$E \left[ u_t \frac{\partial u_t}{\partial \lambda} \right] = \frac{\nu^3 \xi \varsigma (\xi - \varsigma) (\xi + 1)}{(\varsigma + \xi + 2)(\varsigma + \xi + 1)}$$

and in the proof,  $(\xi + \varsigma)^2$  in the first right hand side term of

$$E \left[ u_t \frac{\partial u_t}{\partial \lambda} \right] = \nu^3 (\xi + \varsigma)^2 E[b_t^2(1 - b_t)] - \nu^3 (\xi + \varsigma) E[b_t(1 - b_t)]$$

should be  $2(\xi + \varsigma)$ .

p 216 - (7.17) should be

$$u_{\gamma t} = \frac{1}{4}(x_{1t} + x_{2t})^2 \exp(-2\gamma_{t|t-1}) - \frac{1}{4}(x_{1t} - x_{2t})^2 \exp(2\gamma_{t|t-1}) + \rho_{t|t-1},$$

p 217, right hand side of formula at top of page - each term should be multiplied by  $g$ .

(7.23) should be divided by 2, so the modified score on p 218 is

$$u_{\gamma t} = \frac{1}{8}(x_{1t} + x_{2t})^2 \exp(-2\gamma_{t|t-1}) - \frac{1}{8}(x_{1t} - x_{2t})^2 \exp(2\gamma_{t|t-1}) + \frac{1}{2}x_{1t}x_{2t},$$

(The only substantive difference is the appearance of the term  $x_{1t}x_{2t}$ .)

### Minor corrections

p 24 formula 2.11 - add  $\gamma$  subscript to  $M$ , ie  $M_\gamma$ .

p 63 equation (3.11) -  $\kappa_q$  should be  $\kappa_{q-1}$   
p 139 2 lines above formula at foot of page (4.6) should be (4.2).  
p 146 - in (4.62) delete a bracket, ‘(’, in front of  $y_t$ .  
p 161 above (5.17) -plus after  $\ln \nu$  should be minus.  
P 161 - in the formula above (5.17),  $\nu \xi \lambda_{t|t-1}$  should have a minus sign  
p 192 half-way down page (3.1) should be (6.1)  
Appendix C. Note that it is assumed that  $\mu = 0$  and that  $\lambda_{t|t-1}$  does not  
require a subscript.