

Social Distancing and Supply Disruptions in a Pandemic*

Martin Bodenstein Giancarlo Corsetti Luca Guerrieri
Federal Reserve Board University of Cambridge Federal Reserve Board

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Abstract

We integrate an epidemiological model, augmented with contact and mobility analyses, with a two-sector macroeconomic model, to assess the economic costs of labor supply disruptions in a pandemic. The model is designed to capture key characteristics of the U.S. Input-Output Tables with a core sector that produces intermediate inputs not easily replaceable by the other sectors, possibly subject to minimum-scale requirements. Using epidemiological and mobility data to inform our exercises, we show that the reduction in labor services due to the observed social distancing (spontaneous and mandatory) could explain up to 6-8 percentage points of the roughly 12 percent U.S. GDP contraction in the second quarter of 2020. We show that public measures designed to protect workers in core industries and occupations with tasks that cannot be performed from home, can flatten the epidemiological curve at reduced economic costs—and contain vulnerabilities to supply disruptions vis-à-vis a new surge of infections. Using state-level data for the United States, we provide econometric evidence that spontaneous social distancing was no less costly than mandated social distancing.

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1 Introduction

By the end of March 2020, nearly four months after the first detection of significant coronavirus infections in China, most advanced economies adopted measures restricting people’s movements and activity on their territory, introduced tough controls at their borders, and mandated norms implementing social distancing. If only with some delay, governments converged on the idea that restrictions were required to reduce the human cost of the disease. The decision to adopt mandated restrictions was strongly influenced by early scenario analyses stressing that an uncontrolled and rapid spread of the disease would have overwhelmed national health systems and caused a sharp rise in mortality rates.¹ At the same time, mobility fell precipitously, although not uniformly across locations, as individuals took precautions. During the subsequent months, contagion and death rates, while high, turned out to be much lower than indicated by these early scenario analyses, as social distancing, whether mandated or spontaneous, became widespread practice. At the end of 2020, a new surge associated with more infectious variants of the virus motivated once again the widespread adoption of strict lockdown policies.

Our analysis contributes to the literature on the policy trade-offs raised by a pandemic, with an assessment of the extent to which a large upfront reduction in the supply of labor services caused by the disease and social distancing can weigh on economic activity. Specifically, working in real time in the early months of 2020, we were concerned that labor shortages could have hit industries and parts of the economy that, directly and indirectly, provide essential inputs to production and/or are essential for the economy to run. While it may be difficult to identify precisely which specific industries and activities produce essential inputs and services and hence should be included in the core sector, there are some reasonable choices: distribution services, transportation, sanitation, energy supply, health care services, and food.² Labor shortages that hobble industries in this “core sector” can amplify the

¹ Among the leading papers that formalized this view early on, see [Eichenbaum, Rebelo, and Trabandt \(2020\)](#), [Jones, Philippon, and Venkateswaran \(2020\)](#) and [Alvarez, Argente, and Lippi \(2020\)](#). The literature on the economic effects of the COVID-19 pandemic has grown very fast, see [Atkeson \(2020\)](#), [Alfaro et al. \(2020\)](#), [Baker et al. \(2020\)](#), [Guerrieri et al. \(2020\)](#), and [Koren and Petó \(2020\)](#) among many others.

² For an analysis of production structures and core sectors, see [Carvalho \(2014\)](#) and [Carvalho and Tahbaz-Salehi \(2018\)](#). [Barrot, Grassi, and Sauvagnat \(2020\)](#) offers a sectoral analysis of the effect of the COVID-19

impact economic contraction of a pandemic. First, the services and goods produced by the core sector are not easily substitutable and, second, the production processes in many industries in this sector may be subject to a minimum-scale requirement for labor—i.e., they require a sufficient number of specialized and not easily substitutable employees to show up for work. This amplification mechanisms may not be apparent during normal business cycle fluctuations, but can be expected to become relevant with the scale and timing of a pandemic shock.

We develop a stylized “integrated assessment model for infectious diseases,” which combines a deterministic multi-group epidemiological model with a two-sector economic growth model.³ Using this framework, we can map both the incapacitating effects of the disease on workers and the intensity of social distancing, proxied by mobility data, into the spread of the disease and the number of people able to work as well as the associated contraction in economic activity.

Our main contributions are as follows. First, prior to our quantitative exercises, we motivate our use of mobility data in the model calibration by providing econometric evidence on the epidemiological and economic effects of social distancing. Based on U.S. state-level data for 2020, we find that the reduction in mobility lowered the reproduction rate (defined below) with an elasticity from 3 to 5, and raised initial jobless claims with an elasticity around 0.15. We derive our regression tests from the standard epidemiological SIRD model, proxying contacts using Google mobility data, and instrumenting mobility with either the stay-at-home orders issued by individual U.S. states, or political leanings by state. Strikingly, even though most of the decrease in mobility at the onset of the pandemic was driven by spontaneous social distancing, it was no less costly than stay-at-home orders.

Second, using epidemiological, mobility, and occupational data, we show that the reduction in labor services due to the observed social distancing (spontaneous or mandatory) can explain up to 8 percentage points of the 12 percent output collapse

pandemic.

³ We borrow the term “integrated assessment model” from the literature on climate change to emphasize the importance of linking economics to phenomena that are relevant for the well-being of humankind but that are outside the traditional focus of the economics profession. As in the case of climate change policies, public health policies may have consequences for economic activity that can influence the choices of policymakers.

experienced by the United States in 2020.⁴ Under our working hypotheses on the industry composition and production function in the core sector, almost 2 out of the 8 percentage points of contraction could be attributed to impaired activity in this sector.

To be clear, we are not claiming that supply disruptions were the only mechanism by which the pandemic translated into a sudden large drop in activity in 2020—if anything, our exercise led us to conclude that these disruptions were not as biting as we initially feared. The precipitous fall in demand in early 2020 stemmed from a combination of factors, including: the sudden stop in the consumption of services exposing people to contagion risk (from hospitality to travel and entertainment), the spike in precautionary saving/drop in investment due to the large uncertainty on the medium and long-run effects of the pandemic, and lockdowns and precautionary suspensions of services such non-emergency health care.⁵ To put it simply, in the context of a low demand and mandatory restrictions, possible problems in the supply of, say, public transportation or health services may have not emerged in the open. Yet, we believe it would be wrong to conclude that supply disruptions played no role at the outset of the COVID-19 shock, or that a pandemic would at no time raise issues on the supply side.

A benefit of our focus on the supply side is transparent guidance in the design of social distancing measures. Specifically, our model underscores the benefits of public measures aiming to protect workers in core industries and occupations with tasks that cannot be performed from home. We show that, in a spike of contagion, such measures can flatten the epidemiological curve at reduced economic costs. We argue that, looking at the future, this strategy could contain vulnerabilities to supply disruptions vis-à-vis a new surge of infections—as well as in structuring health measures to accompany the administration of a vaccine.⁶

For the purpose of our analysis, the epidemiological block of our framework

⁴ We calculated this decline relative to the consensus level of GDP in the Blue Chip forecasts published in January 2020, before private forecasters entertained the possibility of a pandemic.

⁵ Jordà, Singh, and Taylor (2020) provide estimates on how pandemics are different from other destructive episodes, such as wars, based on a dataset stretching back to the 14th century. For pandemics, they point to changes in consumption that they attribute to heightened precautionary behavior.

⁶ See, e.g., Correia, Luck, and Verner (2020) for empirical evidence and an account of the beneficial effects of health policies for the case of the 1918 Influenza Epidemic.

includes an extension of the standard susceptible-infective-removed-death (SIRD) model with a homogeneous population to a setting with multiple groups, accounting for the heterogeneous roles that individuals play in the economic production process and accounting for different age groups.⁷ This setup gives us the flexibility to differentiate lockdowns across groups by sector and occupational task. The economic block of our framework, in turn, assumes a low degree of substitutability between core and non-core inputs in producing final output goods, as well as a realistically low degree of worker mobility across sectors (i.e., we set intersectoral mobility to zero). The minimum-scale requirement in the core sector captures the idea that technology in the industries in this sector is such that workers need to operate as members of a team, reflecting the difficulty of replacing team members with specialized skills. By way of example, surgery operations cannot be performed without a complete team of doctors, nurses and technicians; the subway system cannot run if not enough train operators show up for work. A reduction in the number of workers could lead to inefficient work arrangements and/or outright shut-downs of production facilities—so that labor supply and productivity fall in tandem. In addition, we allow for endogenous capacity utilization, investment adjustment costs, and put a lower bound on disinvestment, implying that accumulated capital cannot be consumed.

The two blocks of the model are tied together by the dynamic of the infection (and death) rates, which influence the labor supply. In general, this dynamic is driven by complex interactions of possibly time-varying features of the virus (e.g., mutations) and environmental conditions (e.g., seasonality), with social distancing (spontaneous or mandatory) reducing contacts among people and also influencing the labor supply, and the adoption of precautions conditional on contacts (e.g., masks and hand washing). Because of these complex interactions, the fluctuations in the infection and death rates throughout 2020—with the spread of the pandemic more limited than foreshadowed by early pessimistic scenarios—are a challenge to integrated epidemiological and economic models. We address this challenge by bringing

⁷The origins of the SIRD model and other closely related models of mathematical epidemiology trace back to the seminal contributions of [Kermack and McKendrick \(1927\)](#). [Brauer, Driessche, and Wu \(2008\)](#) offer an introduction to state-of-the-art mathematical epidemiology with numerous models that are more detailed about the dynamics of infectious diseases. However, most of these models feature the SIRD model (or its close cousin the SIS model) at their core.

our model to bear on the dynamic of the (estimated) reproduction rates, calibrating it with mobility data as evidence on contact rates, and estimates of workers who can supply their labor services from home.⁸

The rest of the paper is organized as follows. Section 2 reviews key data for the United States and provides empirical evidence on the effects of social distancing. Section 3 introduces the integrated model, specifying both the epidemiological and the economic elements as well as the structure of social distancing. Section 4 discusses our calibration and solution methods. Section 5 discusses our results on the effects of varying the type and intensity of social distancing measures. Section 6 concludes. Further details on the model and sensitivity analysis are presented in the appendix.

2 Setting the Stage: A Review of Epidemiological Models and Evidence for the United States in 2020

In this section, we set the stage for our analysis by providing and discussing evidence on the dynamic of the COVID-19 pandemic in the United States in the first three quarters of 2020, and the effects of social distancing on the spread of the disease and unemployment across U.S. states. Throughout our analysis, we will make extensive use of mobility data to approximate social distancing and trace its effect on the economy. The evidence in this section is an important preliminary step motivating our theoretical exercises below.

Section 2.1 describes a one-group SIRD model—capturing how a disease spreads by direct person-to-person contact in a population. At this stage, we let individuals differ only with regard to their health status—our baseline model in which individuals differ also with regard to their socioeconomic characteristics will be introduced later. Section 2.2 reviews stylized facts on the diffusion of the disease over time and across states in the United States, including data on mobility and health measures adopted at state level. Drawing on the SIRD model, Section 2.3 specifies a simple econometric

⁸ An alternative strategy would be to modify consumer preferences to model spontaneous social distancing following the lead of, e.g., [Eichenbaum, Rebelo, and Trabandt \(2020\)](#). Our choice is not meant to downplay the importance of investigating theoretically the roots of behavior driving the precautionary reduction in consumption and labor. On the contrary, we see our analysis as strictly complementary to theirs.

framework and provides evidence on the effects of social distancing on the dynamic of the pandemic and employment.

2.1 A Baseline One-Group SIRD Model

The one-group SIRD model in this section follows [Fernández-Villaverde and Jones \(2020\)](#), as we later use their estimates in the validation of our integrated model.⁹ Time is discrete and measured in days. At every instant in time, the total population N is divided into the classes of:

1. susceptible S_t consisting of individuals who can incur the disease but are not yet infected;
2. infective I_t consisting of individuals who are infected and can transmit the disease;
3. resolving R_t consisting of sick individuals who are no longer infective;
4. recovered (or, equivalently, cured) C_t consisting of individuals who have recovered from the disease;
5. deceased D_t consisting of individuals who died from the disease.

This model differs from the standard SIRD model by distinguishing between the infective and the resolving class. [Fernández-Villaverde and Jones \(2020\)](#) found this distinction necessary to obtain a good model fit in their empirical application to U.S. data.

An important assumption of standard SIRD models is that “law of mass action” applies: The rate at which infective and susceptible individuals meet is proportional to their spatial density $S_t I_t$. The effective contact rate per period β_t is the average number of adequate contacts per infective period. An adequate contact of an infective individual is an interaction that results in infection of the other individual if that person is susceptible. Thus, β_t can be expressed as the product of the average of all contacts q_t and the probability of infection (transmission risk) given contact between an infective and a susceptible individual, μ_t .

⁹ Broader introductions to epidemiological modeling are given in [Hethcote \(1989\)](#), [Allen \(1994\)](#), and [Brauer, Driessche, and Wu \(2008\)](#).

It is important to note that the effective contact rate is not constant but can vary over time for a number of reasons. First, an individual's number of contacts, q_t , can drop in a pandemic because of mandated social restrictions (e.g., school closures, closures of shops and restaurants, stay-at-home orders) or voluntary adjustments of behavior (e.g., online shopping instead of in-person shopping, refraining from attending larger gatherings). As both mandated and spontaneous contact restrictions may take place simultaneously, it may be challenging to disentangle their effects on β_t . Nonetheless, restrictions have an impact on the economy regardless of whether they are mandated or spontaneous in nature. Second, the probability of infection given contact between an infectious and a susceptible individual μ_t can vary over time. In the case of COVID-19, this probability is influenced both by human behavior (e.g., masks, keeping sufficient physical distance) and by the characteristics of the virus (e.g., transmission in closed versus open spaces, sensitivity to temperature and seasonality, aggressiveness of the virus strains).

In detail, we write the discrete time SIRD model as:

$$S_{t+1} = S_t - \beta_t S_t I_t / N, \quad (1)$$

$$I_{t+1} = I_t + \beta_t S_t I_t / N - \gamma I_t, \quad (2)$$

$$R_{t+1} = R_t + \gamma I_t - \vartheta R_t, \quad (3)$$

$$C_{t+1} = C_t + (1 - \varpi) \vartheta R_t, \quad (4)$$

$$D_{t+1} = D_t + \varpi \vartheta R_t, \quad (5)$$

$$N = S_t + I_t + R_t + C_t + D_t, \quad (6)$$

with the initial conditions $S_0 > 0$ and $I_0 > 0$. In addition, $S_t \geq 0$, $I_t \geq 0$, and $S_t + I_t \leq 1$. Total new infections at time t are given by $\beta_t S_t I_t / N$. Infections resolve at the Poisson rate γ . A person in the resolving class (R_t) either recovers (C_t) with probability $1 - \varpi$ or dies (D_t) with probability ϖ . The recovery rate is denoted by ϑ . In principle, the recovery rate and the death rate could also be time-varying to reflect advancements in medical treatment as the pandemic progresses.

2.2 The Dynamic of the COVID-19 Spread in the United States

Conditional on a constant contact rate β , with an empirically relevant reproduction rate equal to 2, a mainstream estimate for the onset of the pandemic, almost the entire population is infected in a matter of months. According to leading scenarios debated in March 2020, for instance, it could not be ruled out that between 15 and 20 percent of the U.S. population could have simultaneously developed symptoms, and that, over a short time frame, 20 percent of these symptomatic individuals would have required hospitalization.¹⁰ These developments would have put devastating pressure on the health care system of any country.

Scenarios conditional on a constant β played a crucial role in motivating stark health measures in many countries—for this reason, we will study this type of scenario as a benchmark reference below. Remarkably, however, these grim developments did not come to pass. Figure 1 superimposes data for the spread of COVID-19 in the United States, death rates and confirmed cases, and data on the timing of stay-at-home orders and changes in residential mobility—culled from cellphones, as captured in Google’s mobility reports, and reflecting both trips towards residential addresses and time spent at those addresses.¹¹

Tracking the spread of COVID-19 is no easy feat. Even the best available data are subject to important drawbacks. As Figure 1 shows, confirmed new cases surged in March 2020, reached a first peak in early April, a second peak in mid-July and climbed back up through the fall. Using confirmed new cases to measure the intensity of the pandemic is challenging since severe rationing of testing at the beginning of the pandemic kept the data artificially low. Data on death rates do not suffer from that problem and confirm at least three cycles for the spread of the disease. However, the relationship between the spread of the disease and death rates can also vary as new treatment protocols are developed or the age composition of infected individuals evolve, given that older individuals experience greater mortality rates. The middle

¹⁰ For instance, see [Ferguson et al. \(2020\)](#).

¹¹ The data for death rates and confirmed cases are from [JHU CSSE \(2020\)](#), also see [Dong, Du, and Gardner \(2020\)](#). The data on stay-at-home orders are from [Raifman et al. \(2020\)](#). The mobility data are from [Google LLC \(2020\)](#).

panel of the figure shows the reproduction rate for the model in Equations (1)-(6) estimated by [Fernández-Villaverde and Jones \(2020\)](#) based on data on death rates. The solid black line shows the overall estimate for the United States. Two cycles are clearly visible in the estimates of the reproduction rate. The state-level estimates show much greater variation, as indicated by the point-wise maximum and minimum dashed red lines for these estimates.

Figure 1 also shows that stay-at-home orders were put in place at different points in time across states, roughly within a three week window from mid-March to early April.¹² These orders had a median duration of six weeks, but the duration also varied considerably by state. Twelve states did not impose stay-at-home orders. In the states that did, the shortest orders lasted three weeks and the longest, for California, was still standing in parts of the state at the time of writing.

The figure suggests that social distancing contributed significantly to slowing down the spread of the disease. It also shows that mobility measures capturing time spent at home ramped up even before the imposition of stay-at-home orders at the regional level. We will take advantage of the timing of these events to gain some insight on the relative role of spontaneous vs. mandated social distancing in driving the evolution of the disease.

2.3 The Effects of Social Distancing

In this section we provide evidence that social distancing, be it spontaneous or mandatory, has comparable epidemiological and economic effects. Specifically, based on the epidemiological model, we derive and apply two empirical tests of the hypothesis that contacts, as proxied by mobility data, have an effect on the reproduction rate and the initial jobless claims. First, we will focus on changes in mobility in response to stay-at-home orders, using a difference-in-difference approach. Then we will investigate the dynamic evolution of contagion in the two-week period in March that preceded any mandatory measure, based on cross-sectional evidence.

Several other papers have sized empirically the economic effects of mandated social distancing, including [Allcott et al. \(2020\)](#) and [Coibion, Gorodnichenko, and](#)

¹²The earliest stay-at-home order started in California on March 19.

Weber (2020). Our approach is closest to Gupta et al. (2020), who also use a difference in difference approach to size the effects on the labor market. Our specific approach helps us distinguish between the direct effects of the social-distancing policies through reduction in mobility and outcomes related to spontaneous social distances predating the policies.¹³ Goolsbee and Syverson (2021) also rely on a difference in difference estimation method but use more capillary data at the local level. Nonetheless, their results on the economic effects of mandated social distancing are broadly in line with ours.

For both tests below, we derive our regression framework from the SIRD model described in Section 2.1. In the SIRD framework, the status of the pandemic is summarized by the reproduction rate

$$R_{0,t} = \frac{1}{\gamma} \beta_t. \quad (7)$$

where the effective contact rate β_t is the product of contacts q_t , normalized to 1, and the probability of transmission, μ_t . We can therefore express the reproduction rate as

$$\ln(R_{0,t}) = -\ln(\gamma) + \ln(\mu_t) + \ln(q_t - r_t) \quad (8)$$

where the term r_t represents policy restrictions that can reduce the level of contacts. We will use this equation to derive a panel regression and a cross-sectional test.¹⁴ Atkeson, Kopecy, and Zha (2021) provide framework consistent with ours to decompose the reproduction rate but allow for a feedback mechanism between the reproduction and infection rates.

¹³ See Atkeson, Kopecy, and Zha (2021) for an extension of the canonical SIR model that incorporates spontaneous feedback from disease prevalence to disease transmission.

¹⁴ Alternative approaches to estimating the effects of mandated social distancing measures are offered by Chernozhukov, Kasahara, and Schrimpf (2021) and Huang (2020). They focus on epidemiological effects, whereas we are also interested in a comparison of the epidemiological benefits and of the economic consequences of mandated and spontaneous social distancing.

2.3.1 Mandated Social Distancing: A Panel Regression Approach

The relationship between the reproduction rate and contacts in Equation 8 can be mapped into the following panel regression equation:

$$\ln(R_{0,s,t}) = FE_m + bm_{s,t} + FE_s + e_{s,t}. \quad (9)$$

where the subscript s denotes the geographical region and the term $R_{0,s,t}$ is the regional counterpart to the aggregate $R_{0,t}$ in Equation 8. The dependent variable in our baseline, consistent with the model in Section 2.1, is the reproduction rate estimated by Fernández-Villaverde and Jones (2020). We average the daily estimates by these authors to the weekly frequency and use readings for the 48 U.S. states in their dataset and the District of Columbia.¹⁵ We use monthly fixed effects, FE_m , to capture the time-varying probability of transmission μ_t , which might depend on taking precautions such as frequent hand-washing and mask-wearing that have become more prevalent with the spread of the virus.¹⁶ We proxy contacts $q_t - r_t$ at the regional level with the term $m_{s,t}$, the Google index for residential mobility in percent deviation from its value at the beginning of 2020, also averaged to the weekly frequency. The term FE_s denotes regional-level fixed effects, which allow for regional characteristics to influence the relationship between contacts and mobility. Finally, $e_{s,t}$ is a stochastic term in the relationship between contacts and mobility. Our main interest is the regression coefficient b . An important restriction imposed by our regression framework is that this coefficient does not vary across regions.

We estimate Equation 9 by two-stage least squares, using a dummy for the stay-at-home orders as an instrument for residential mobility. To lessen endogeneity concerns we lag the dummy for the stay-at-home orders by one week. At the first stage, we also allow for monthly and regional fixed effects. The estimation sample has starting points that vary by region, in line with regional variation in the spread of the disease. The earliest estimates of the reproduction rate are for the state of Washington, starting on March 12, 2020. By contrast, estimates of the reproduction

¹⁵ The dataset of Fernández-Villaverde and Jones (2020) excludes Wyoming and Montana.

¹⁶ The framework of Atkeson, Kopecky, and Zha (2021) captures these effects as a time-varying wedge.

rate for Hawaii only start on August 7, 2020. The end point for the estimation sample across all regions is September 28, 2020. Overall, the sample includes 1204 observations.

Our estimates of Equation 9, first and second stage, are shown in Table 1. In the table, Column 1 indicates that, on average, stay-at-home orders push up the mobility index 1.85 percent. Returning to the table, Column 2 shows that a 1 percent increase in residential mobility reduces the reproduction rate by about 3.5 percent, all else equal. Putting the two estimates in columns 1 and 2 together, on average, the stay-at-home orders led to a decline in the reproduction rate of about $1.85 \times 3.5 \approx 6.5$ percent. In other words, starting from a basic reproduction rate of 2, the stay-at-home order would reduce it to about 1.9. One may note that, at its peak, the index of residential mobility increased by about 20 percent (reflecting an increase in time spent at home). Even if all states had enacted stay-at-home orders, our estimates would attribute only 1.85 percentage points of this increase to those orders. Accordingly the great majority of the 20 percent increase was linked to spontaneous social distancing.

To gauge the effects of the stay-at-home orders on initial unemployment claims, we use a regression framework analogous to that of Equation 9. We consider

$$U_{0,s,t+1} = FE_m + b_u m_{s,t} + FE_s + e_{s,t+1}, \quad (10)$$

where the term $U_{0,s,t}$ represents initial jobless claims as a share of the working age population in region s at time t . For the sake of comparison, we select an estimation sample with exactly the same span of the sample for the regression of the reproduction rate. We also estimate Equation 10 by two-stage least squares, using a dummy for the stay-at-home orders as an instrument for residential mobility. Once again, using standard Durbin and Wu-Hausman tests, we fail to reject the null hypothesis that the instrument is exogenous. This time, probability values for the tests are of 0.13 and 0.14, respectively. Connecting the estimates in columns (1) and (3) of Table 1, the regression results point to an increase in the unemployment rate of roughly 0.3 ($1.85 \times 0.153 \approx 0.3$) percentage point for every week that the stay-at-home orders

were in force. With a median duration of 6 weeks and the orders applying to much of the country, they could have accounted for an increase in the unemployment rate of about 2 percentage points.

2.3.2 Spontaneous Social Distancing: A Cross-Sectional Approach

To study the effect of spontaneous social distancing, we consider a two-week period before the imposition of any stay-at-home order—the 14-day period through March 17, which is two days before the first stay-at-home order went into effect in California. The evidence reviewed above suggests that much of the reduction in mobility had already occurred by the time mandatory rules started to be imposed. Yet, this initial mobility reduction was far from homogeneous across states.

A useful observation for our purpose is by [Gollwitzer et al. \(2020\)](#), who note that individual political leanings influence social distancing practices, and through these practices also influence health outcomes. We design a second test of our hypothesis building on this observation. Namely, we instrument mobility with political leanings by U.S. state, as captured in the share of the vote for the Republican candidate in the 2016 presidential election. Given our focus on the first part of March, before the introduction of mandatory measures, we collapse the time dimension of our initial panel regression and rely only on the cross-sectional variation at the state level.

Starting from the regression framework in Equation 9, we now difference the specification between two points in time on the same month. Focusing on the regression for reproduction rate, this differencing yields

$$\ln(R_{0,t,s}) - \ln(R_{0,t-h,s}) = b(m_{s,t} - m_{s,t-h}) + e_{s,t} - e_{s,t-h}. \quad (11)$$

(We proceed analogously for initial jobless claims using equation 10 as a starting point.)

We again estimate the elasticity coefficient b by two-stage least squares. In the first stage we use political leanings to instrument the change in mobility between two points in time. In the second stage, we regress our dependent variable—either the reproduction rate or the initial claims—on the fitted change in residential mo-

bility. In this exercise, we cannot use the estimates of the reproduction rate in [Fernández-Villaverde and Jones \(2020\)](#), since these start in the second half of March for most regions. We rely instead on the estimates from [Systrom, Vladek, and Krieger \(2020\)](#), which start earlier and are based on an adaptation of the estimation method of [Bettencourt and Ribeiro \(2008\)](#). The middle and bottom panels of [Figure 1](#) offer a comparison of these alternative estimates of the reproduction rate when aggregated at the national level.

The estimates of the reproduction rate from [Systrom, Vladek, and Krieger \(2020\)](#) cover all 50 U.S. states and the District of Columbia. The starting date for these estimates varies by state, in line with the differential spread of the disease. The earliest estimates are for February 19, 2020 for the state of Washington, whereas, at the other end of the spectrum, estimates for Alaska, Idaho, and West Virginia only start on March 8, 2020.¹⁷

The message from our new exercise is loud and clear. As shown in [Table 2](#), [Column 1](#), there is a strong correlation between political leanings and the change in mobility. In [columns 2 and 3](#), the null hypothesis that the coefficient on the instrumented mobility is 0 can be rejected at standard significance levels, despite the fact that we only have 51 observations. The elasticity of initial jobless claims with respect to mobility in [column 3](#) of this table, at about 0.17, is remarkably close to the analogous elasticity in [column 3](#) of [Table 1](#), which is approximately 0.15. This finding indicates that the economic costs of changes in mobility are comparable, regardless of whether the changes are driven by mandated or spontaneous measures. However, it could still be the case that for comparable costs, the spontaneous measures could have induced a bigger decline in the reproduction rate. Moving back to [Table 1](#) for the panel regression instrumented with stay-at-home orders, [Column 2](#) shows an elasticity of the reproduction rate with respect to mobility of about -3.5. By contrast the analogous estimate in [Column 2](#) of [Table 2](#) is about -2.3, which implies a lower effectiveness of spontaneous measures in reducing the reproduction rate relative to mandated measures.¹⁸

¹⁷ Given the later start of estimates for the reproduction rate, for Alaska, Idaho, and West Virginia we use a shorter window of nine days when computing the changes in [Equation 11](#).

¹⁸ For our comparison we used estimates based on different datasets for the mandated and spontaneous mea-

In sum, we have produced evidence that, despite the fact that spontaneous measures at the onset of the pandemic drove the bulk of the reduction in mobility, they were no less costly than mandated measures, even when controlling for their impact on the reproduction rate. This result is an original contribution of our analysis. While subsets of our results have also been documented by related analyses, the value added from our study consists of comparing the effects of mandated social distancing with the effects of spontaneous distancing, on both epidemiological and economic indicators.

3 A Four-Group, Two Sector Integrated Model

In this section, we motivate and present our integrated assessment model for infectious diseases. This model combines a deterministic compartmental SIRD model of epidemiology with four population groups, and a two-sector economic growth model.

As we have seen above, epidemiological models attempt to map the complex transmission interactions of infectious diseases in a population into a formal mathematical structure that can describe the large scale dynamics. To integrate epidemiological and economic models, we have to make assumptions about the interaction of the spread of the disease with economic activity. In our framework, we allow for three channels. First, if at least some of the individuals who have fallen ill from the disease cannot work, the aggregate labor supply shrinks temporarily and reduces economic activity. Second, social distancing to control the spread of the infectious disease either prevents individuals from conducting their work altogether or limits their productivity (e.g., by imposing inefficient home-office arrangements). Again, the reduction in effective labor causes economic activity to fall and, if the social distancing is implemented over a long time period, a decline in investment activity may cushion the near-term fall in consumption but add persistence to the economic repercussions. Third, in our two-sector economic growth model, it matters greatly for

ures, the datasets of [Fernández-Villaverde and Jones \(2020\)](#) and of [Systrom, Vladek, and Krieger \(2020\)](#), respectively. We can also estimate the elasticity of the reproduction rate with respect to mobility for mandated measures using the dataset of [Systrom, Vladek, and Krieger \(2020\)](#) and find an even more sizable elasticity of about -5.1.

economic activity how the health measures affect labor supply across across sectors.

We should stress from the start a key difference between our approach and leading contributions, pioneered by [Eichenbaum, Rebelo, and Trabandt \(2020\)](#), that redefine preferences to capture how agents reduce consumption or labor supply in view of contagion risk when engaging in these activities. Instead of modifying preferences to account for the unobservable spontaneous precautionary behavior in social interactions, we calibrate our integrated model with evidence on differential contact rates implied by engaging in different activities, to gain insight on how the observed reduction in contacts, proxied by mobility, can affect economic activity via supply disruptions. By no means is this choice meant to downplay the importance of modelling and investigating theoretically the roots of behavior driving the precautionary reduction in consumption and labor. On the contrary, we see the two modelling strategies as complementary lines of research.

In our approach, we treat variations in mobility from the data equally regardless of whether they are driven by spontaneous decision or mandated measures. The evidence in the previous section, showing that both types of changes in mobility had comparable effects on the reproduction rate and unemployment, lends empirical support to our choice.

Our approach nonetheless places demands on the epidemiological model. In particular, relative to the model presented in the previous section, we need to track different population groups depending on their roles in the economy. This multi-group model is described in the next section.

3.1 The Epidemiological Block of the Integrated Model: A Four-Group SIRD Model

As a key bridge between epidemiology and economics, we expand the SIRD model presented in Section 2.1 by splitting the population N in four groups. The size of group $j \in \{1, 2, 3, 4\}$ is denoted by N_j with $N_1 + N_2 + N_3 + N_4 = N$. The members of each group are homogeneous and share specific socioeconomic characteristics. The members of groups 1 and 2 are in the labor force and are employed in sectors 1 and

2, respectively. The members of the third group, the young, attend school and do not work. Similarly, the members of the last group, the old, do not work either.

Relative to the one-group model, another important innovation in our four-group model is the possibility that at time T^{vac} a highly effective vaccine becomes available. For each of the four group of the population we now have susceptible, infective, resolving, recovered (cured), deceased, as well as a subgroup of vaccinated, denoted, respectively, $S_{j,t}, I_{j,t}, R_{j,t}, C_{j,t}, D_{j,t}, V_{j,t}$ with $S_{j,t} + I_{j,t} + R_{j,t} + C_{j,t} + D_{j,t} + V_{j,t} = N_j$. Notably, both the average number of contacts per person and the probability of transmission can differ across groups, so that the effective contact rate transmission can be group-dependent.¹⁹ We refer to β_t as the matrix of effective contacts in the multi-group SIRD model. The elements $\beta_{j,k,t}$ of β_t are the group-dependent contact rates which measure the probability that a susceptible person in group j meets an infective person from group k and becomes infective.

As far as there is no vaccine, susceptible individuals remain susceptible until they become infected. Once a vaccine becomes available at time T^{vac} —assuming that the vaccines is fully effective—the subpopulation of susceptibles shrinks as individuals are vaccinated. We denote by $\psi_{j,t}$ the vaccination rate for group j at time t . Note that it is $\psi_{j,t} = 0$ for $t < T^{vac}$ for all j .

The system of equations for the four-group SIRD model is given by:

$$S_{j,t+1} - S_{j,t} = -S_{j,t} \sum_{k=1}^4 \beta_{j,k,t} I_{k,t} / N_k - \psi_{j,t} S_{j,t}, \quad (12)$$

$$I_{j,t+1} - I_{j,t} = S_{j,t} \sum_{k=1}^4 \beta_{j,k,t} I_{k,t} / N_k - \gamma_j I_{j,t}, \quad (13)$$

$$R_{j,t+1} - R_{j,t} = \gamma_j I_{j,t} - \vartheta R_{j,t}, \quad (14)$$

$$C_{j,t+1} - C_{j,t} = (1 - \varpi_j) \vartheta R_{j,t}, \quad (15)$$

$$D_{j,t+1} - D_{j,t} = \varpi_j \vartheta R_{j,t}, \quad (16)$$

$$V_{j,t+1} - V_{j,t} = \psi_{j,t} S_{j,t}, \quad (17)$$

with $j \in \{1, 2, 3, 4\}$. We discuss the parameterization of the effective contact rates

¹⁹ A straightforward example of two groups with different transmission coefficients are hospital patients and medical personnel.

in detail below.

3.2 The Macroeconomic Block of the Integrated Model: A Two-Sector Model

Individuals live in identical households that pool consumption risk across the different household members, i.e., the composition of each household reflects the relative group sizes in the population. However, we do not allow labor to be substitutable across sectors. Absent social distancing, all susceptible and recovered individuals work. Infective individuals may or may not be symptomatic: we assume that symptomatic individuals do not work. We describe the connection between the economic and the epidemiological model in the next section.

Our model comprises two intermediate sectors, Sector 1 and Sector 2. Individuals in Group 1 provide labor services inelastically to firms in Sector 1. Individuals in Group 2 provide labor services inelastically to firms in Sector 2. Individuals in groups 3 and 4, the young and the old, are not in the labor force. Final goods are produced with inputs from the two intermediate sectors with a constant elasticity of substitution function. These inputs are imperfect substitutes for each other.²⁰ The two sectors differ by their production structure. In Sector 1, labor inputs are subject to a minimum scale requirement. This scale requirement is a simple way to capture the specialized skills of different workers, all of which are necessary to produce a certain product. Larger labor shortfalls make it more likely that production will be impaired by the absence of essential members of a team. We abstract from modeling the interaction of capital with the labor input in Sector 1. We have in mind production structures in which capital cannot easily compensate for shortfalls in the labor input. For example, if doctors and nurses do not show up for work, it seems unlikely that adjustments could be made to compensate for their absence. By contrast, with Sector 2, we are attempting to capture production processes in which the utilization of capital services can be more easily adapted, and in which labor

²⁰ Krueger, Uhlig, and Xie (2020) also bridge an epidemiological model and a two-sector economic model, building on the setup of Eichenbaum, Rebelo, and Trabandt (2020). In the model of Krueger, Uhlig, and Xie (2020), different contact rates distinguish each sector. Furthermore, labor is the only input into production and labor mobility across sectors helps blunt the economic impact of the pandemic.

inputs are more readily substitutable for capital services.

Households maximize consumption and supply two types of labor, $l_{1,t}$ and $l_{2,t}$ inelastically. Households also rent capital services $u_t k_{t-1}$ to firms in Sector 2, where u_t captures variable capacity utilization that can also be adjusted for those services. The utility function of households is:

$$U_t = E_t \sum_{i=0}^{\infty} \theta^i \log(c_{t+i} - \kappa c_{t+i-1}). \quad (18)$$

Households choose streams of consumption, investment, capital and utilization to maximize utility subject to the budget constraint

$$c_t + i_t = w_{1,t} l_{1,t} + w_{2,t} l_{2,t} + r_{k,t} u_t k_{t-1} - \nu_0 \frac{u_t^{1+\nu}}{1+\nu} - \frac{\zeta}{2} \frac{(i_t - i_{t-1})^2}{i_{t-1}}, \quad (19)$$

where the term $-\nu_0 \frac{u_t^{1+\nu}}{1+\nu}$ captures costs from adjusting capital utilization. The parameter ν_0 allows us to normalize utilization to 1 in the steady state, whereas the parameter ν determines how costly it is to change utilization. The term $-\frac{\zeta}{2} \frac{(i_t - i_{t-1})^2}{i_{t-1}}$ captures costs of adjusting investment, with these costs governed by the parameter ζ . Households' utility maximization is also subject to the law of motion for capital, given by

$$k_t = (1 - \delta)k_{t-1} + i_t, \quad (20)$$

and to a threshold level of investment,

$$i_t \geq \phi i, \quad (21)$$

where ϕi denotes a fraction of steady-state investment. Notice that when $\phi = 0$, Equation 21 implies the irreversibility of capital.

Moving to the description of the production sector, firms in Sector 1 use labor $l_{1,t}$ to produce the good $v_{1,t}$ and charge the price $p_{1,t}$. The production function is given by

$$v_{1,t} = \eta (l_{1,t} - \chi). \quad (22)$$

Firms in Sector 2 use capital k_{t-1} and labor $l_{2,t}$ to produce good $v_{2,t}$,

$$v_{2,t} = (u_t k_{t-1}^\alpha) l_{2,t}^{1-\alpha}. \quad (23)$$

The final output good is a composite of the goods 1 and 2:

$$y_t = \left((1 - \omega)^{\frac{\rho}{1+\rho}} (v_{1,t})^{\frac{1}{1+\rho}} + \omega^{\frac{\rho}{1+\rho}} (v_{2,t})^{\frac{1}{1+\rho}} \right)^{1+\rho}. \quad (24)$$

3.3 Integrating the Epidemiological and the Macroeconomic Model

The dynamics of the epidemiological and the macroeconomic models are interwoven. On the one hand, the virus and mitigation measures—both spontaneous and mandated—directly reduce economic activity: Symptomatic sick individuals may not work. The labor supply may also decline if healthy individuals decide not to work either because of workplace closures or because of their own choosing to reduce their exposure to the virus. Similar considerations can also precipitate a contraction in consumption. On the other hand, individuals’ ability and willingness to engage in economic activity has direct implications for the spread of the virus. People who, for whichever reason, work from home or not at all have fewer relevant contacts that could result in an infection. The lower risk of infection is reflected in the decline in the effective contact rate β_t .

3.3.1 Dynamics of the Effective Contact Rate

Similar to other recent contributions on the macroeconomics of epidemics, in our setting β_t is sensitive to economic conditions and choices.²¹ However, rather than positing a direct functional relationship between economic variables and the effective contact rate β_t , our functional form for β_t is consistent with the key feature of the “law of mass action” assumed in the SIRD and other popular epidemiological models. Under this law, the rate at which infective and susceptible individuals meet

²¹ See for example, Alvarez, Argente, and Lippi (2020), Eichenbaum, Rebelo, and Trabandt (2020), and Kaplan, Moll, and Violante (2020).

is proportional to their spatial density. We specify a mapping from spatial density to economic variables, which accounts for the fact that not all reductions in spatial density translate necessarily into a reduction of economic activity.

Recall that β_t is defined as the product of the matrix of average contacts q_t and the transmission risk μ_t . Epidemiologists have carefully studied people’s social contact patterns to understand the spread of infectious diseases. Importantly, contacts differ by location and age. The POLYMOD study, one influential study of social contacts, allows to derive matrices for the contacts between the members of different age groups in four location settings: home (h), school (s), work (w), and other (o).²² The time-invariant matrix q^l with $l \in \{h, s, w, o\}$ informs about the number of contacts that a typical member of each demographic group has with the members of each demographic group. Absent contact restrictions, the average contact matrix aggregated over locations satisfies

$$q_t = q^h + q^s + q^w + q^o. \quad (25)$$

Spontaneous and mandatory restrictions reduce social contacts through lowering spatial density. Consistent with the law of mass action, we assume the quadratic form

$$q_t = q^h + \sum_{l=\{s,h,o\}} (1 - r_t^l)q^l(1 - r_t^l)' \quad (26)$$

where the row vector r_t^l denotes the reduction in the spatial marginal density of each demographic group. Time-variation in r_t^l induces time-variation in the average contact matrix aggregated over locations q_t even if the underlying contact matrices are constant. Equation 26 foreshadows our calibration assumption that contacts at home between family members cannot be reduced by mitigation measures. Of course, the economic costs can differ across types of restrictions.

While data on contact rates and contact restrictions are available, little is known about the factors influencing the transmission risk μ_t of the coronavirus. Viruses mutate and they can become more or less contagious. Appropriate hygiene, masks,

²²The POLYMOD study, discussed in [Mossong et al. \(2008\)](#), reports contact patterns for several European countries.

and keeping proper physical distance seem to lower the transmission risk according to the Center for Disease Control and Prevention. The transmission also appears to be higher indoors than outdoors; increased outside activity during the warmer months of the year may thus lower temporarily the transmission risk. Absent direct quantitative evidence how these factors affect the transmission risk, we shy away from specifying a functional form that describes the evolution of the transmission risk over time. Instead, we treat μ_t as an exogenous variable.

3.3.2 Disease Spread, Disease Management and the Labor Supply

A pandemic may cause economic costs and disruptions through different channels. Our focus is on how infections and contact restrictions impair the labor supply—a key driver of economic activity. Specifically, we link the evolution of the labor supply explicitly to infections and contact restrictions using data on mobility and the ability to work from home. Our modelling choice does not mean that we view other channels, such as a drop in “social consumption” (restaurants and hospitality) as unimportant. Rather, it reflects the difficulty to establish a data-oriented link between these channel and the pandemic.²³ We should nonetheless note that our approach also accounts for a reduction in consumption triggered by changes in the labor supply, wage income and investment.

Without the disease, the labor supply in each sector is

$$l_{j,t} = N_j, \tag{27}$$

for $j \in [1, 2]$ for all t . As the disease starts spreading, we assume that sick and symptomatic individuals that are in the resolving state, $R_{j,t}$, do not work. In addition, the labor force of each sector is reduced by deaths. Hence, denoting with ι the share

²³ In the case of consumption, note that social contact studies provide little detail on consumption-related contacts. Even if we classify all “other contacts” as consumption-related, neither theory nor data provide clear guidance for how reductions in consumption-related contacts map into reductions in consumption and thus economic activity. For example, a wider use of technology (online transactions, delivery and pickup services) or product substitution (food at home vs. food away from home) may imply little change in consumption expenses even as consumers manage to reduce consumption-related contacts. The closing of providers of consumption services to reduce consumption-related contacts mechanically implies a reduction in the consumption of services. But such a decline in consumption could also be viewed as supply-driven and linked to a reduction in labor.

of resolving individuals who are asymptomatic, the labor supply in sector j satisfies

$$l_{j,t} = N_j - D_{j,t} - (1 - \iota) R_{j,t}, \quad (28)$$

for $j \in [1, 2]$.

We have already shown how spontaneous and mandatory restrictions reduce contacts, see Equation (26). Consistent with our focus on potential supply disruptions from the disease, we posit that contact restrictions directly relate to economic activity only by affecting the supply of labor services. As defined earlier, $r_{j,t}^w$ denotes the share of individuals in group j , that stop going to the workplace per effects of contact restrictions. Now, not all work restrictions imply a fall in labor services, since some jobs can be carried out from home. Assuming that contact restrictions apply to all individuals in a group regardless of their health status, then, the labor supply in sector j is given by

$$l_{j,t} = N_j - D_{j,t} - \max[r_{j,t}^w - v_j, 0] (N_j - D_{j,t}) - \min[r_{j,t}^w, v_j] (1 - \iota) R_{j,t} - (1 - r_{j,t}^w) (1 - \iota) R_{j,t}. \quad (29)$$

In Equation 29, the contraction in the supply of labor services (in addition to deaths) is accounted for by three terms. A first term, $\max[r_{j,t}^w - v_j, 0] (N_j - D_{j,t})$, nets out the services provided by individuals in group j with contact restrictions, where v_j is the share of individuals in group j who can continue working from home. The second and third terms net out individuals who are sick and symptomatic. The term $\min[r_{j,t}^w, v_j] (1 - \iota) R_{j,t}$ is the number of sick and symptomatic individuals in group j who are under restrictions and are working from home. The term $(1 - r_{j,t}^w) (1 - \iota) R_{j,t}$ is the number of individuals in group j who get sick and are symptomatic but are not under restrictions.

3.3.3 The Special Case of a One-Sector Macroeconomic Model

We conclude noting how our four-group/two-sector model can be simplified and made comparable with other models in the literature. Trivially, the four-group SIRD model readily collapses to a three-group model when we impose that all the shares

pertaining to Group 1 are zero, i.e., $S_{1,t} = I_{1,t} = R_{1,t} = C_{1,t} = D_{1,t} = N_1 = 0$. For comparability with the literature, it is also useful to keep the non-working-age population (Groups 3 and 4), separate from the others. By the same token, our two-sector model collapses to a prototypical one-sector real business cycle model when we impose that the quasi-share parameter ω in Equation 24 is one.

4 Calibration and Solution

In this section, we present our calibration, summarized in Table 3, distinguishing parameters relevant for the SIRD model and for the two-sector economic model. We then discuss our solution method.

4.1 The Parameters of the SIRD model

We take many of the parameters to calibrate the epidemiological model from the work by [Fernández-Villaverde and Jones \(2020\)](#), the study on which we built our econometric work in Section 2.2. Infectiousness resolves at the Poisson rate $\gamma_j = 0.2$ in all four groups, i.e., within five days. Individuals move into the recovering class at the rate $\vartheta = 0.1$ from which they either recover with probability $1 - \varpi_j = 0.99$ or die with probability $\varpi_j = 0.1$. Hence, after 10 about days, an individual either is cured or deceased. Again, we assume the probability of death to be identical across groups.

To parameterize the effective contact rate we first use data derived from the POLYMOD study to build contact matrices by age-group and location. We then combine the information on contact matrices with estimates for the reproduction number to obtain estimates for the transmission rate. The POLYMOD study, funded by the European Union, aims to strengthen public health decision making in Europe through the development, standardisation and application of mathematical, risk assessment and economic models of infectious diseases. [Mossong et al. \(2008\)](#) offer a detailed discussion. In particular, the POLYMOD study offers data on contacts by age-group and location for a number of European countries.

[Prem, Cook, and Jit \(2017\)](#) and [Prem et al. \(2020\)](#) project the data from the

POLYMOD study to a large set of countries including the United States. We aggregate the contact data by location and age provided in Prem, Cook, and Jit (2017) into three age groups (young, middle-aged, and old). The matrices are displayed in Table 4. The young and the middle-aged have considerably more total contacts than the old and most of their contacts are with members of their own age group. For the young more than half of the contacts occur at school and for the middle-aged about half of the contacts occur at work. Contacts in locations other than school, work and home include contacts during commuting, shopping and leisure activities. Other contacts account for an important fraction of total contacts only for the old. We assume the same contact patterns for middle-aged individuals regardless of their sector of employment.²⁴

To obtain an estimate of the transmission risk we use the contact matrices and estimates of the basic reproduction number. Note that in the multi-group SIRD model the reproduction rate is given by the spectral radius of the matrix $\mu_t q_t \frac{1}{\gamma}$ where q_t is the sum over the contact matrices by location. We set μ_t to match the empirical value of the reproduction number given the contact patterns and the infection rate γ . Initially, the transmission probability μ_0 equals 0.023 which is consistent with an initial value of 2 of the reproduction number absent restrictions on mobility.

It is worth reiterating that the calibration of our SIRD model is daily. In order to link the results from the epidemiological model to the macroeconomic models, we average the results of the epidemiological model across thirty-day intervals.

4.2 The Parameters of the Economic Model

The relative sizes of the four groups are informed by the employment to population ratio, the age distribution of the U.S. population, and the employment share in the core sector. We set the combined size of Group 1 and Group 2, $N_1 + N_2$, at about 0.6 (or 60 percent of the total population), in line with data from the U.S. Bureau of Labor Statistics (BLS) for the employment-to-population ratio. Group 3 (the young)

²⁴The contact patterns for the United States are qualitatively similar to those reported for other advanced economies. The average of total contacts per individual for the United States is similar to the average for Italy and somewhat above the average for Korea and the UK. The POLYMOD study implies significantly lower contacts for Germany reflecting much lower contacts at schools and the workplace.

accounts for about 25 percent of the population and Group 4 (the old) accounts for about 15 percent of the population.

The individual group sizes N_1 and N_2 reflect the employment share of the group of industries in the economy that we deem essential and that are reported in Table 5. The data on value added come from the tables on GDP by Industry of the Bureau of Economic Analysis (BEA). The employment shares reflect hours worked by industry in the Productivity Release of the BLS. The shares reported in the table are for 2018, the latest year for which data are available at the time of writing. The total share of employment for the industries listed in the table is about 38 percent. Identifying the individuals working in the essential industries as the Group 1 individuals in the SIRD model we set $N_1 = 0.6 \times 0.38 \approx 0.23$. Hence, Group 2 is of size $N_2 \approx 0.37$.

The total share of GDP for the industries listed in the table is about 27 percent. We fix the quasi-share parameter ω so that the value added of Sector 1 in the steady state is the same percent of total output in the model, i.e., denoting steady-state variables by omitting the time subscript, $\frac{p_1 v_1}{y_1} = 0.27$.

The unit of time for the economic model is set to 1 month. We set the discount factor θ to $1 - \frac{4}{100}/12$, implying an annualized interest rate of 4 percent in the steady state. The depreciation rate δ is set to $\frac{1}{10}/12$, implying an annual depreciation rate of 10 percent. The parameters governing consumption habits κ is set to 0.6, in line with estimates for medium-scale macro models such as [Smets and Wouters \(2007\)](#). We set the parameter α governing the share of capital in the production function of Sector 2 to 0.3. The elasticity of substitution between factor inputs is $\frac{1}{3}$, implying a choice of $\rho = \frac{1}{1-\frac{1}{3}}$ as derived in the appendix. We set the parameter ν governing the elasticity of capacity utilization to 0.01, as in [Christiano, Eichenbaum, and Evans \(2005\)](#). The parameter ϕ is equal to 0, implying that investment, once installed as capital, is irreversible. In line with the broad range in [Altig et al. \(2011\)](#) and the literature, we set to 10 the parameter ζ , which governs the costs of adjustment for investment.

We set χ , the minimum scale parameter for the production function of Sector 1, to $\frac{6}{10}$ times l_1 , implying that $\frac{4}{10}$ of the steady state labor input for sector 1 is essential for production. The scaling parameter η is set to $\frac{10}{4}$, offsetting the reduction

in productivity implied by our choice of the minimum-scale parameter in the steady state. This choice for η leaves the steady state production level unchanged relative to a case without a minimum scale (i.e., when χ is 0). The appendix discusses how our calibration of the scale parameters allows the model to match the observed collapse in economic activity when we feed into the model a series of labor supply shocks that replicates the reduction in labor inputs implied by the increase in unemployment from March through October 2020, relative to the unemployment level in February 2020.

4.3 Cross-model Parameters

In our model, the macroeconomic cost of inaction is driven by the reduction in the labor supply caused by the inability of symptomatic infective individuals to work until recovered. To calculate the reduction in labor supply, we need to rely on an estimate of the asymptomatic infected individuals. A study of the passengers of the Diamond Princess cruise ship provides useful guidance. As reported in [Russell et al. \(2020\)](#), about half of the passengers that tested positive for the virus were asymptomatic. The asymptomatic share was also found to be different by age group. We use a 40 percent estimate that applies to passengers of working age, i.e. $\iota = 0.4$. Given that labor supply is exogenous in our economic model, the fall in labor supply becomes more acute as the infective share increases.

When we study the effects of social distancing measures, we need to allow for the possibility that a fraction of the individuals subject to lockdown measures may still be able to work from home. To estimate the fraction of individuals who can do so, we use the American Time Use Survey of the BLS. According to survey data for 2018, the latest available at the time of writing, about 30 percent of American workers can work from home. The survey also provides differential rates by industry. Mapping the coarser industry categories onto our industry choices for Sector 1 as listed in [Table 5](#), we extrapolate that 15 percent of individuals in Group 1 can work from home, compared to 40 percent of individuals in Group 2. Thus, we set $v_1 = 0.15$ and $v_2 = 0.4$.

4.4 Solution Method

The solution method has three important characteristics: First, it allows for a solution of the SIRD model that is exact up to numerical precision; second, it conveys the expected path of the labor supply in each group to the economic model as a set of predetermined conditions, following the numerical approach detailed in the appendix of [Bodenstein, Guerrieri, and Gust \(2013\)](#); and third, it resolves the complication of the occasionally binding constraints, implied by capital irreversibility, with a regime switching approach following [Guerrieri and Iacoviello \(2015\)](#). The modular solution approach has the advantage of allowing us to consider extensions of either module without complicating the solution of the other.

5 Simulation Results

We are now ready to use our model. We carry out two main exercises. In a first exercise (the next subsection), we show that labor supply disruption can go a long way to explain a contraction in output similar to the one experienced by the United States at the beginning of the pandemic. To this end, we calibrate our model using mobility data and estimates of the share of workers that can work from home.

In our second exercise, we repeat the analysis replacing the estimates of mobility with a lockdown, which we design drawing on the main lessons from our integrated model. From our supply-side perspective, health measures can reduce economic disruptions to the extent that they are successful in protecting workers in the core sector from the infection externality when other workers and people circulate without restrictions. For comparison, we also build a scenario with “inaction”, under which, counterfactually, there is no social distancing at all. This is meant to highlight the potentially large economic consequences of the disease when its spread is unmitigated by any, spontaneous or mandatory, social distancing.

We emphasize from the start that our main goal is assessing the economic consequences of potential *supply disruptions from labor market shortages*. Important economic costs may stem from shifts in demand patterns, associated with large reallocation costs, in the presence of nominal, financial and other frictions. However, a

shock of the size and nature of a pandemic raises a unique set of questions concerning how the supply structure of an economy can continue to work when confronting an abrupt reduction in the scale of production. This reduction is what our model is designed to capture.

5.1 Labor Supply and Output Disruptions

In this first set of simulations, our model tracks data on the observed reduction in mobility from the beginning of March through the end of October 2020, together with labor market and occupational data. Our goal is to bring our integrated model to bear on the estimated path of the reproduction rate over the same period.

Figure 2 shows an abrupt decline in the workplace mobility measure from [Google LLC \(2020\)](#) at the onset of the pandemic. Over the second half of March, workplace mobility was cut in half. Thereafter, over April and May, workplace mobility partially bounced back but remained 30 percent below pre-pandemic levels through the end of October. The figure also shows that the decline in workplace mobility was mirrored by an increase in the residential mobility measure from [Google LLC \(2020\)](#)—basically proxying for the time spent at home.

For our analysis, we need to map the decline in mobility into a reduction in contacts through the workplace and a reduction in labor inputs. Accordingly, we need to take a stand on the share of workers who continued to work from home. As discussed in the calibration section, estimates based on the BLS American Time Use Survey point to about 30 percent of the work force being able to continue working from home. As a baseline, we can treat any reduction in mobility in excess of this 30 percent mark as a reduction in labor inputs. For instance, at the peak of 50 percent reduction in workplace contacts, we will assume that the fall in labor input amounts to $50-30=20$ percentage points. This approach is backed by estimates of office occupancy rates based on entry card swipes, which also show a precipitous decline in the second half of March 2020 to *de minimis* levels, followed by only a modest rebound in occupancy rates through the end of October 2020. Overall, the evidence suggests that a large share of workers who could switch to working from

home, did so.²⁵

In our simulations, we impose that the path of the reproduction rate implied by our simulations is close to realistic estimates of this rate.²⁶ The top panel of Figure 3 shows again the estimate of the reproduction rate from Fernández-Villaverde and Jones (2020), the solid black line, matched by construction in our simulation. This panel also shows the reproduction rate implied by our epidemiological model, incorporating the changes in mobility discussed above but without overriding the probability of transmission needed to match the estimates of Fernández-Villaverde and Jones (2020). The panel clarifies that the mobility changes go a long way in capturing the empirically relevant reproduction rate.

We stress that our model-implied path for the reproduction rate includes not only the reduction in workplace contacts, but also a reduction in non-work activities/contacts for all population groups (whether or not in the work force), which we assume to be of the same magnitude as the reduction in work contacts. This assumption is buttressed by the reduction in non-work mobility measures indicative of social distancing across different population groups. Looking back to Figure 2, note that the reduction of mobility towards retail outlets and transit hubs is strikingly close to the reduction in mobility towards workplaces. Moreover, in our simulations, we set school contacts to 0 from the beginning of April to the beginning of August, in line with the widespread school closures in the United States during this period. After August, we allow for an increase in school contacts, but only by half the pre-COVID-19 levels, to account for a partial re-opening of schools across the country.

The paths for the reproduction rate that our model generates based on this stylized set of assumptions is remarkably close to estimates based on deaths from COVID-19. The estimated path does dip below the model-implied path for most of the period (apart from a window in July and August). It is worth reiterating here

²⁵ For instance see coverage of office occupancy rates based on Kastle card swipes in the Wall Street Journal “Companies Tiptoeing Back to the Office Encounter Legal Minefield” published on November 16, 2020.

²⁶ As explained in the calibration section, we set the probability of transmission given contact, μ_t , to match the empirical value of the reproduction number given the contact patterns and the infection rate, γ . This is important: if the model missed in this dimension, an excessively high reproduction rate would lead to a significant share of infected symptomatic workers, that would counterfactually amplify the drop in the labor input.

that mobility and contacts, however important, are not the only factors affecting the spread of the disease. The rate of disease transmission may fall if people wear masks (a precaution that has become more prevalent over time), and/or in response to seasonal factors. With good weather, people may spend more time outside, except when very high temperatures push them back inside, in air-conditioned spaces.

The top two panels of Figure 4 show the model-implied progression of the infection at the quarterly frequency. The number of infected individuals reaches a peak in the second quarter. Even at this peak, however, the reduction in labor supply attributable to the inability to work of symptomatic infected individuals was too small to have a significant effect on the overall labor supply.²⁷

The economic scenarios generated by our model are shown in the bottom four panels of Figure 4, contrasting the predictions of our one- and the two-sector version of the model. While both models have qualitatively similar implications for the course of economic activity, there is a marked quantitative difference. In the one-sector model, the output collapse in the second quarter is about 6 percent. In our two sector model, the collapse is one fourth larger, 8 percent. Both models predict large contractions—a significant share of the observed decline in GDP in the United States in the second quarter of 2020 (which clearly reflects a number of other forces). The difference between the one- and the two-sector models is also apparent in the paths of utilization, consumption and investment.

What explains these differences is the fact that, in our two-sector version of the model, the consequences of a fall in the labor inputs in the essential sector are amplified by the non-monotonic feature of the production function—the minimum scale assumption implies a significant fall in overall labor productivity. Because of this specific feature of the model, the distribution of labor supply cuts across sectors is of first-order importance. In our simulations, we take the conservative approach of adjusting the sectoral labor cuts so to keep the reduction in value added in the second quarter of 2020 balanced across sectors, as shown in Figure 5. The rationale for this assumption is that the share of work from home is different across the two

²⁷ As shown in the figure, the number of deaths plateaus at 300,000 after 6 quarters from the start of the sample period. This is because in our simulations the reproduction rate becomes constant at the level estimated for the end of October, which was close to 1.

sectors. If we applied the mobility data homogeneously across sectors, the reduction in labor inputs would be heavily skewed toward the essential sector. By keeping the reduction in value added balanced across the two sectors, our distribution of labor cuts actually minimizes the drop in aggregate output—as a way to reduce the risk of overstating the incidence of supply shortages in disrupting economic activity.

The main takeaway is that supply disruptions in the wake of a pandemic could play a non-negligible role in the collapse in GDP—even if these are not amplified by a drop in the productivity of the core-sector (as shown by our one-sector model); and even when the spread of the disease remains contained (possibly because of social distancing) and the economic costs of social distancing are mitigated by a widespread switch to working from home. Larger supply disruptions may of course result from a recrudescence of the disease motivating widespread and stricter lockdowns—which would also increase the distance between the one- and the two-sector model.²⁸

5.2 The Effects of Mandated Social Distancing

In this section, we discuss how the tradeoffs between health and economic outcomes can be improved by adopting *mandated* social distancing measures that recognize the need to protect the core sector of the economy. In simulations that follow, changes in the reproduction rate (from the initial level of 2) come about exclusively from the reduction in contacts implied by mandated social distancing measures. For comparison, we also bring forward a scenario under a constant reproduction rate, i.e., conditional on no social distancing. This scenario will be labeled “inaction.” We note that the inaction scenario arguably weighed on policymakers’ perception of the disease in March 2020 (see [Ferguson et al. \(2020\)](#)). Indeed, in the absence of a clear understanding of the factors that could influence the transmission of the disease, early debates were sometimes conducted under the assumption that, absent policy intervention, the reproduction rate would stay constant at its initial level.

It is worth stressing that we intentionally steer away from “optimal policy” anal-

²⁸ The main focus of our exercise is on labor supply disruptions and its effects on overall productivity. As the model misses in other dimensions of the current crisis, such as omitting shifts in the composition of demand, in our simulation economic activity tends to rebound more quickly than observed.

ysis, as it would require a richer model as well as taking a stand on such parameters as the value of human lives. However, our analysis draws on key principles that are also building blocks in optimal policy exercises. Specifically, we consider policy measures that are meant to internalize the infection externality from individual interactions, not efficiently accounted for by optimizing individuals on their own (see, e.g., [Eichenbaum, Rebelo, and Trabandt \(2020\)](#)).

5.2.1 A Baseline Social-distancing Configuration

To minimize the supply disruption of a lockdown, the health measures we consider in our experiment target first and foremost workers who are able to continue supplying their labor services from home. In line with the American Time Use Survey, conducted by the Bureau of Labor Statistics, the share of the labor force that can work from home is 15 percent of workers in Group 1 (the group that supplies labor to the core sector), and 40 percent of workers in Group 2 (the group that supplies labor to the other sector). Accounting for the sizes of Group 1 and Group 2, combined, this boils down to subject about 30 percent of the labor force to a complete lockdown. A second set of restrictive measures are then targeted to reduce contacts between core-sector workers who cannot provide their services from home, and the general population. Consistently, we extend our health measures to individuals not in the labor force, those in Group 3 and Group 4, up to restricting 30 percent of group members, the same proportion used for the working population. With a lockdown imposed on 1/3 of the total population, keeping the reproduction rate unchanged for the population not subject to these measures, lifting the restrictions after 12 months would lead to a resurgence of the pandemic, but one that, due to the building up of herd immunity at a controlled pace, would spread more slowly.

The health consequences of the lockdown policy just described are illustrated by the top two panels of [Figure 6](#). The policy successfully flattens the infection curve: the peak of the infection share of recovering individuals drops from about 8 percent to about 3 percent—admittedly still high relative to the capacity constraint of healthcare systems, even when taking account of the fact that not all infected individuals experience symptoms. A notable result is that the health outcomes of

individuals are similar in Group 1 and 2, despite the fact that workers in the Group 1 continue working “on the road” in higher proportion than workers in Group 2. The near-equalization of infection rates results from the way our lockdown measures internalize the infection externality—the higher degree of social distancing in Group 2 and a high share of population under a lockdown helps shield individuals in Group 1.

Panels 5 through 8 of the figure contrast the economic consequences of mandated social distancing with a counterfactual scenario of “inaction.” The reason to call attention to this counterfactual scenario is that it allows to highlight the potentially high upfront economic costs of the rapid peak in the disease due to labor supply disruptions from (i) the inability of the symptomatic ill to continue working (in the aggregate this may become relevant when the disease spreads at high rates); and (ii) the reduction in labor supply due to deaths of individuals in the labor force. In our work, we further stress the indirect, potentially significant costs from supply constraints on the economy that follows a large contraction of the core sector.

Comparing these scenarios, the importance of smoothing out the peak of the infection curve is apparent. Under our mandated social distancing baseline, the peak contraction in output is less than one half relative to the case of inaction. Key to this result is that, while the social distancing policy compresses the trough for value added similarly in both sectors, Sector 1 remains more active relative to the scenario without intervention.

Another notable result in the figure is that, independently of mandated social distancing measures, the pandemic has persistent economic consequences. These reflect both the death toll on the size of labor force, and the fact that a smaller labor force leads to a persistent reduction in the productivity of the essential sector, weighing on final output, consumption, and investment—not only in the aggregate but also in per capita terms.

In sum, the key takeaway from our exercise is that lockdowns can be structured to reduce the risks of large supply disruption in the economy. In particular, lockdown policies should be stricter on workers in the non-core sector and non-active population, and targeted specifically at workers who could reasonably keep performing

their occupational tasks from home. Such combination of measures is successful to the extent that they address the infection externality where it has more economic bite, i.e., they keep the infection rate among the workers in core industries low.

5.3 Waiting for a Vaccine

The rest of this section uses the model to address the costs of a long lockdown put in place in view of the availability of a vaccine, including some sensitivity analysis motivated by the considerable uncertainty surrounding the parameters of the model.

The prospects of a vaccine in the non-distant future from the eruption of the pandemic raise the benefits of investing in social distancing, keeping contagion rates to a level that can be effectively dealt with by the national health system until the immunization programs can be rolled out. The lockdown measures studied in the previous sections do not fully qualify: they smooth out the infection curve considerably, but do not go insofar as preventing persistent hikes in the share of infected/recovering individuals—which in all likelihood remains well above the response capacity of the health care system. We thus turn our attention to mandated measures extended and modified to keep the share of infected individuals low enough to avoid overtaxing the health care system.

Specifically, we target our lockdown to keep the share of recovering individuals in the population below 1 percent until a vaccine becomes available, set to 9 months after the onset of the pandemic.²⁹ At that point, the immunization campaign starts. We assume that the vaccine is perfectly protective and that 10 percent of the population is inoculated each month.

In the logic of our model, the cost of containing the share of the infected population can be significantly reduced by extending the lockdown on non-working population (groups 3 and 4) and by imposing measures that reduce non-work contacts more aggressively. Relative to our baseline example discussed in Section 5.2.1, we increase the share of the population under lockdown in groups 3 and 4 from 30 percent to 40 percent—and posit that non-work contacts can be reduced in this greater proportion

²⁹ We use the 1 percent share for illustrative purposes. Alternatively one could target the peak incidence of the disease explicitly to the capacity of the health care sector as in [Moghadas et al. \(2020\)](#).

for all groups. Results are shown in Figure 7, whereas the lockdown measures are relaxed after 12 months, as immunity is then built with immunization. Provided that all the measures remain effective over this long time span, the results in the figure suggest that well-structured health interventions are in principle able to reduce both the spread of the disease and the economic consequences.

In our baseline, the assessment of the economic costs of a strict lockdown waiting for a vaccine is arguably overly optimistic. Our model abstracts from many factors that can amplify the crisis via demand and income disruptions. But even keeping focus exclusively on labor supply disruptions, the assessment crucially depends on both the degree of effectiveness of (and compliance in) a lockdown, and the characteristics of the COVID-19 virus. We investigate robustness in these two dimensions running two exercises below. In each of these two exercises, we maintain the basic design features of our baseline simulation in Figure 7. Namely, we still target a population share of recovering individuals below 1 percent until the arrival of the vaccine 9 months after the onset of the pandemic, and assume the same monthly rate of vaccination of 10 percent.

So far, we have assumed that the social distancing measures can bring the contact rates to 0. As robustness, we follow [Alvarez, Argente, and Lippi \(2020\)](#), who consider a lower effectiveness of social distancing, only reducing contacts by 80 percent. Under this assumption, with our lockdown measures in place, the peak of the population share of recovering individuals would rise from just under 1 percent, to about 2 percent. A target below 1 percent would then require a tighter lockdown. For instance, the target could be met by raising the share of individuals in groups 1 and 2 under lockdown, to about 20 and 50 percent, respectively—while also extending the lockdown to 40 percent of the nonworking population for 12 months.³⁰ With these stricter measures in place, however, the economy would experience a drop in output of about 8 percent for the duration of the wait for a vaccine.³¹

The cost of waiting for a vaccine would also be higher with an increase in the probability of transmission due to a virus mutation. The new variant of the COVID-

³⁰ We still constrain the share of individuals under lockdown in Group 3 to match the share for groups 1 and 2 combined.

³¹ See Figure A.3 in the appendix.

19 virus identified in the United Kingdom at the end of 2020 is estimated to be up to 70 percent more transmissible. Mapping this estimate into a change in the probability of transmission given contacts, would imply a rise in the reproduction rate from 2 to 3.3. With our baseline lockdown in place, the higher reproduction rate would be sufficient to raise the share of recovering individuals to about 8 percent, nearly as high as in a scenario of inaction. The goal of keeping this share below 1 percent in this case would require more drastic measures. For instance, the goal could be achieved by placing under lockdown 40 and 90 percent of individuals in Group 1 and Group 2, respectively, and about 80 percent of individuals outside the labor force. Furthermore, the lockdown would have to be extended for a longer period, 15 months, since a greater share of the population would have to be vaccinated to achieve herd immunity. The economic consequences would be dire. According to our model, the reduction in output would be as large as 50 percent before herd immunity is reached and the lockdown is lifted. The contraction in investment would be so large to cause the capital irreversibility constraint to bind—in turn amplifying the contraction in consumption.³²

6 Conclusion

A precipitous decline in employment brought about by the spread of an infectious disease can have outside economic costs if it ends up compromising linkages in the production structure that are critical for the working of the economy as a whole. We study the aggregate effects of supply disruptions potentially brought about by a disease, specifying a two-sector model featuring a set of industries that produce core inputs used by all the other industries. Core inputs are both poorly substitutable with other inputs, and produced subject to a minimum scale of production.

Our integrated assessment framework suggests that the way an unchecked spread of a pandemic can damage the economy is through labor drawdowns in core industries that could undermine efficient production in other sectors and, thus, aggregate economic activity. This is an economic argument for social distancing, distinct from

³² See Figure A.4 in the appendix.

the argument stressing the need to reduce the loss of human life resulting from congestion overwhelming hospitals and health care systems. Simulations of our integrated assessment model suggest that even moderate mandated social distancing may actually improve economic outcomes.

In our framework, the direct economic cost of the disease stems from the inability of symptomatic infected individuals to continue working and the drop in labor services due to spontaneous or mandated social distancing. Additional indirect costs come from the constraint that malfunctioning core industries may place on other industries via input-output linkages. Social distancing measures modulated to shield essential economic linkages can buffet the fall in aggregate economic activity effectively and without compromising the primary goal of flattening the infection curve. The experiments we consider in this paper consist of applying social distancing measures proportionally more to the non-working-age population, and workers in non-core industries and to occupations that involve tasks that can be performed from home. These measures work through a key epidemiological externality that ends up protecting workers in the core industries.

Calibrated with mobility data and estimates of the incidence of work-from-home, our model comes close to matching the dynamic evolution of COVID-19 in the United States through the summer of 2020. The spread of the disease, while pervasive, was substantially less dramatic than suggested by some early epidemiological studies, which underestimated the mitigating effects of the widespread adoption of both spontaneous and mandated social distancing on the reproduction rate. We investigate empirically the epidemiological benefits and economic costs of social distancing at the onset of the pandemic. We derive our empirical framework from the standard model, proxying contacts using Google mobility data, and instrumenting mobility with either the stay-at-home orders issued by individual U.S. states, or political leanings by state. Our results suggest that, at the margin, changes in mobility through the first quarters of 2020 in the United States had significant effects on both reproduction rates and initial jobless claims. Strikingly, spontaneous social distancing was no less costly than stay-at-home orders.

This paper was first drafted at the very beginning of the COVID-19 pandemic,

conditional on early epidemiological scenarios of a rapid spread of the disease. Ex post, the rate of contagion, while high, was not as dramatic and initially feared. Supply disruptions did not emerge as a systemic binding constraint. By no means does this observation downplay the need to model carefully the resilience of production network and analyze its vulnerabilities. While supply chains remained remarkably resilient in 2020, the sharp and sudden drop in demand and the temporary suspension in the supply of services (e.g., in the healthcare sector) may have hidden the potential difficulties in producing core services when there are not enough workers to meet the minimum scale of production.

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Table 1: The Effects of Stay-at-Home Orders

	(1)	(2)	(3)
	Res. Mobility	Reproduction Rate	Init. Unemp Claims
	2sls 1 st step	2sls 2 nd step	2sls 2 nd step
Stay-at-home orders	1.850** (0.000)		
Residential mobility index		-3.502* (0.010)	0.153** (0.000)
r ²	0.918	0.153	0.610
N	1204	1204	1204

p-values in parentheses

⁺ *p* < 0.1, * *p* < 0.05, ** *p* < 0.01

All the regressions are run with data at the weekly frequency and include state and month fixed effects. A state-by-state dummy that takes a value of 1 if a stay-at-home order is in force and zero otherwise is the instrument for the Google residential mobility index in the 2-stage-least-squares regressions in columns (2) and (3). The results in column (2) are based on the reproduction rate from the dataset of [Fernández-Villaverde and Jones \(2020\)](#).

Table 2: The Effects of Spontaneous Social Distancing

	(1)	(2)	(3)
	% Change Res. Mobility	% Change R	PPt. Change Init. Claims
	2sls 1 st step	2sls 2 nd step	2sls 2 nd step
% Republican Votes in 2016	-0.189** (0.000)		
PPt. Change Res. Mobility		-2.268 ⁺ (0.099)	0.168** (0.003)
r ²	0.607	0.0439	0.140
N	51	51	51

p-values in parentheses

⁺ *p* < 0.1, * *p* < 0.05, ** *p* < 0.01

Political leanings, as measured by the share of votes for the Republican presidential candidate in the 2016 election are the instrument for the Google residential mobility index in the 2-stage-least-squares regressions in columns (2) and (3). The results in column (2) are based on the reproduction rate from the Rt.Live dataset of [System, Vladek, and Krieger \(2020\)](#). These regressions focus on the two-week period prior to the enactment of any state-level stay-at-home orders.

Table 3: Parameters for the Integrated Assessment Model

Parameter	Used to Determine	Parameter	Used to Determine
$\mu_0 = 0.023$	initial transmission probability (daily)	$\gamma = 0.2$	resolution rate (daily)
$\vartheta = 0.1$	recovery rate	$\varpi = 0.01$	death rate (daily)
$\iota = 0.40$	share of symptomatic infectives	$\psi = 0$	vaccination rate
$N_1 = 0.23$	size Group 1	$N_2 = 0.37$	size Group 2
$N_3 = 0.25$	size Group 3	$N_4 = 0.15$	size Group 4
$v_1 = 0.15$	share working from home Sector/Group 1	$v_2 = 0.40$	share working from home Sector/Group 2
$\theta = 1 - \frac{4}{100}/12$	discount factor (monthly)	$\delta = \frac{1}{10}/12$	capital depreciation rate (monthly)
$\kappa = 0.6$	habit persistence	$\nu = 0.001$	elasticity capacity utilization
$\phi = 0$	degree of capital reversibility	$1 - \omega = 0.27$	quasi-share value added Sector 1
$\eta = \frac{10}{4}$	scaling parameter Sector 1	$\chi = \frac{6}{10}N_1$	minimum scale Sector 1
$\rho = \frac{1}{1-1/3}$	substitution elasticity Sectors 1 and 2	$\alpha = 0.3$	share capital in production Sector 2
$\zeta = 10$	investment adjustment cost		

Note: This table summarizes the parameterization of the baseline integrated assessment model.

Table 4: Contacts by Age and Location

contacts at home (young, middle-aged, old):

$$q^h = \begin{pmatrix} 1.7544 & 1.7649 & 1.3082 \\ 1.7649 & 1.9108 & 1.2287 \\ 1.3082 & 1.2287 & 0.5111 \end{pmatrix}$$

contacts at work (young, middle-aged, old):

$$q^w = \begin{pmatrix} 0.0312 & 0.1769 & 0.0030 \\ 0.1769 & 5.3887 & 0.1489 \\ 0.0030 & 0.1489 & 0.0023 \end{pmatrix}$$

contacts at school (young, middle-aged, old):

$$q^s = \begin{pmatrix} 6.9261 & 0.1733 & 0.0037 \\ 0.1733 & 0.0819 & 0.0051 \\ 0.0037 & 0.0051 & 0.0038 \end{pmatrix}$$

other contacts (young, middle-aged, old):

$$q^o = \begin{pmatrix} 2.8675 & 1.5398 & 0.2267 \\ 1.5398 & 3.9481 & 1.2921 \\ 0.2267 & 1.2921 & 0.8290 \end{pmatrix}$$

total contacts (without reductions):

$$q^h + q^w + q^s + q^o = \begin{pmatrix} 11.5792 & 3.6548 & 1.5416 \\ 3.6548 & 11.3295 & 2.6747 \\ 1.5416 & 2.6747 & 1.3461 \end{pmatrix}$$

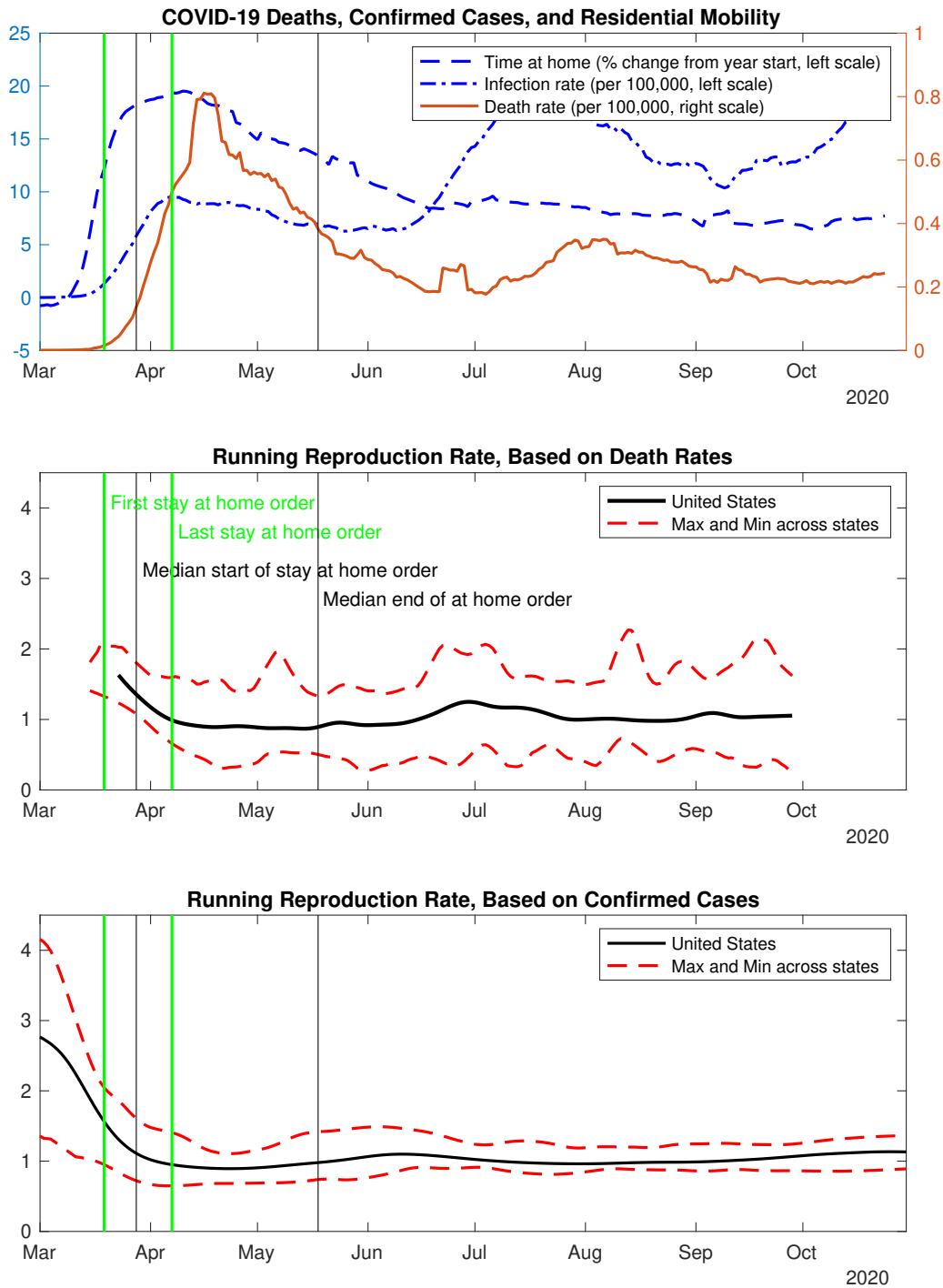
Note: Contacts by age—ordered as young (0-19), middle-aged (20-64), and old (65+)—were obtained by aggregation over more detailed data provided in [Prem, Cook, and Jit \(2017\)](#) and [Prem et al. \(2020\)](#). We present the contacts for middle-aged working individuals not disaggregated by sectors

Table 5: The Core Sector: Share of GDP and of Employment

Line	Sector	Value Added,\$ bn.	Percent of GDP	Percent of Employment
3	Agriculture, forestry, fishing, and hunting	166.5	0.81	2.65
10	Utilities	325.9	1.58	0.52
26	Food and beverage and tobacco products	268.9	1.31	1.86
31	Petroleum and coal products	172.2	0.84	0.12
37	Food and beverage stores	156.4	0.76	2.2
40	Transportation and warehousing	658.1	3.2	5.27
76	Health care and social assistance	1536.9	7.47	8.66
91	Federal government, general services	729.0	3.54	0.88
96	State government, general services	1600.5	7.78	15.38
	Total	5614.4	27.29	37.56

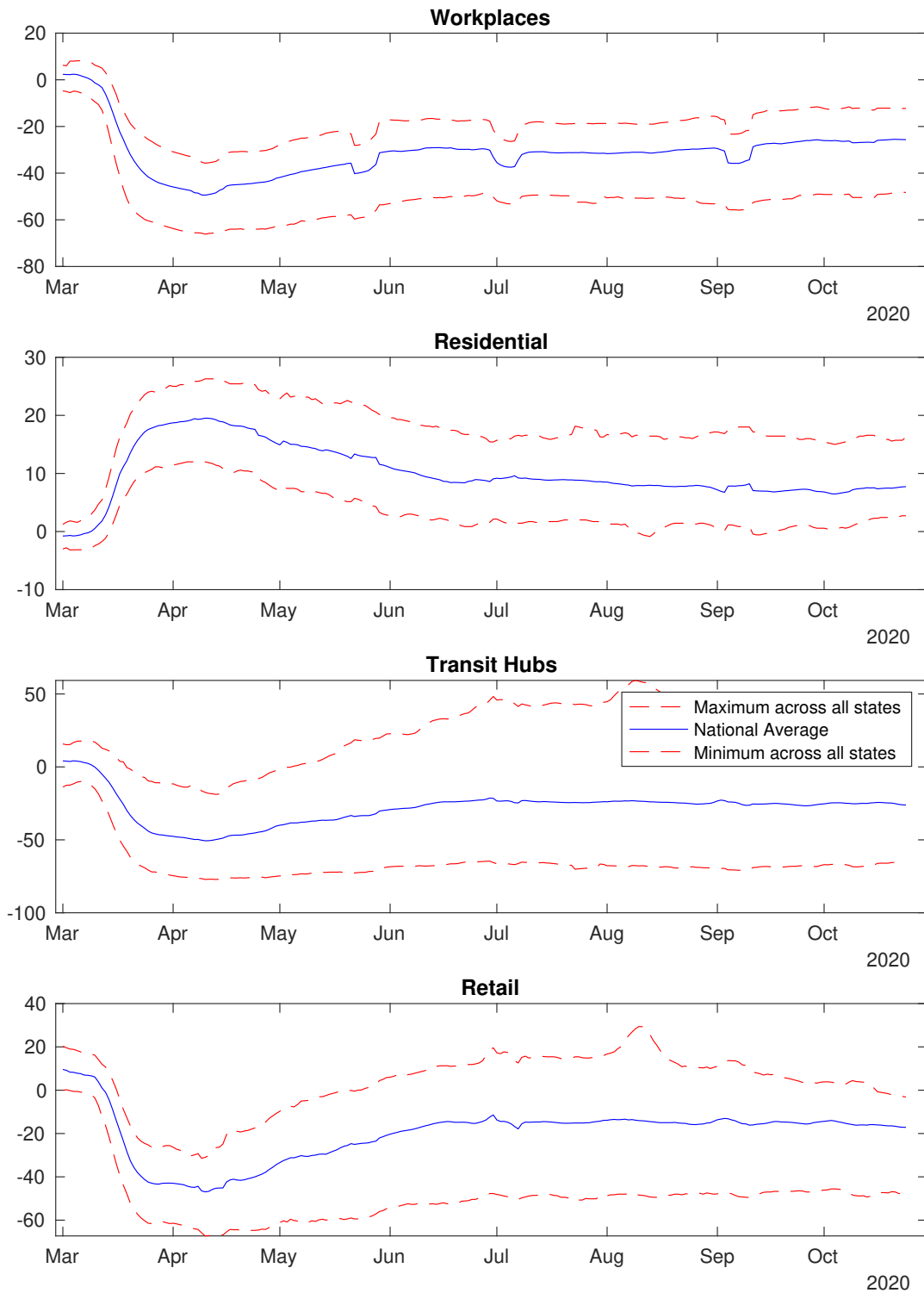
Source: Authors' calculations based on Bureau of Economic Analysis, GDP by Industry, and Bureau of Labor Statistics, Productivity Release.

Figure 1: Stay-at-Home Orders, Mobility, COVID19 Death and Infection Rates — 7-Day Moving Average



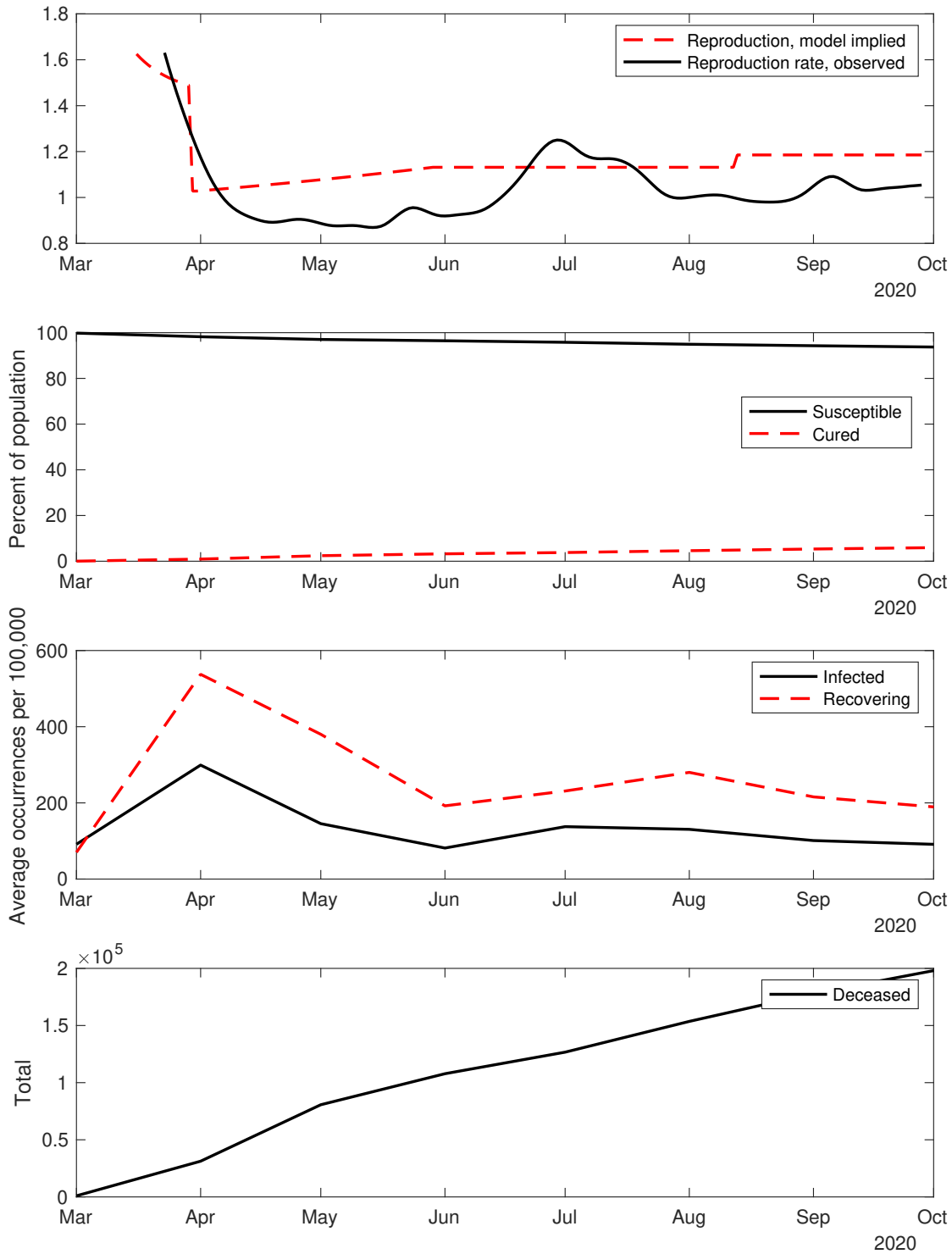
Note: The vertical lines denoting key dates are repeated in each panel. Sources: The data for death rates and confirmed cases are from [JHU CSSE \(2020\)](#). The data on stay-at-home orders are from [Raifman et al. \(2020\)](#). The residential mobility data are from [Google LLC \(2020\)](#). The estimates of the reproduction rate based on deaths are from [Fernández-Villaverde and Jones \(2020\)](#). The estimates of the reproduction rate based on confirmed cases are from [System, Vladek, and Krieger \(2020\)](#).

Figure 2: Workplace and Residential Mobility—7-Day Moving Average



Note: The dips in workplace mobility at the end of May, beginning of July and end of September correspond to national holidays. Their effects are prolonged by the moving average.
 Source: [Google LLC \(2020\)](#).

Figure 3: Dynamics in the SIRD Model



Note: The paths shown are aggregates for the total population. The observed reproduction rate is used in the model simulations and to back out the paths in the bottom three panels. The model-implied paths are generated varying the number of contacts in line with the residential mobility measure from [Google LLC \(2020\)](#) and school closures but keeping the probability of contagion given contacts unchanged from its baseline value. The paths in the top panel are daily. All other panels show monthly averages of daily series.

Figure 4: Aggregate Economic Consequences of COVID-19: Comparing One-Sector and Two-Sector Models

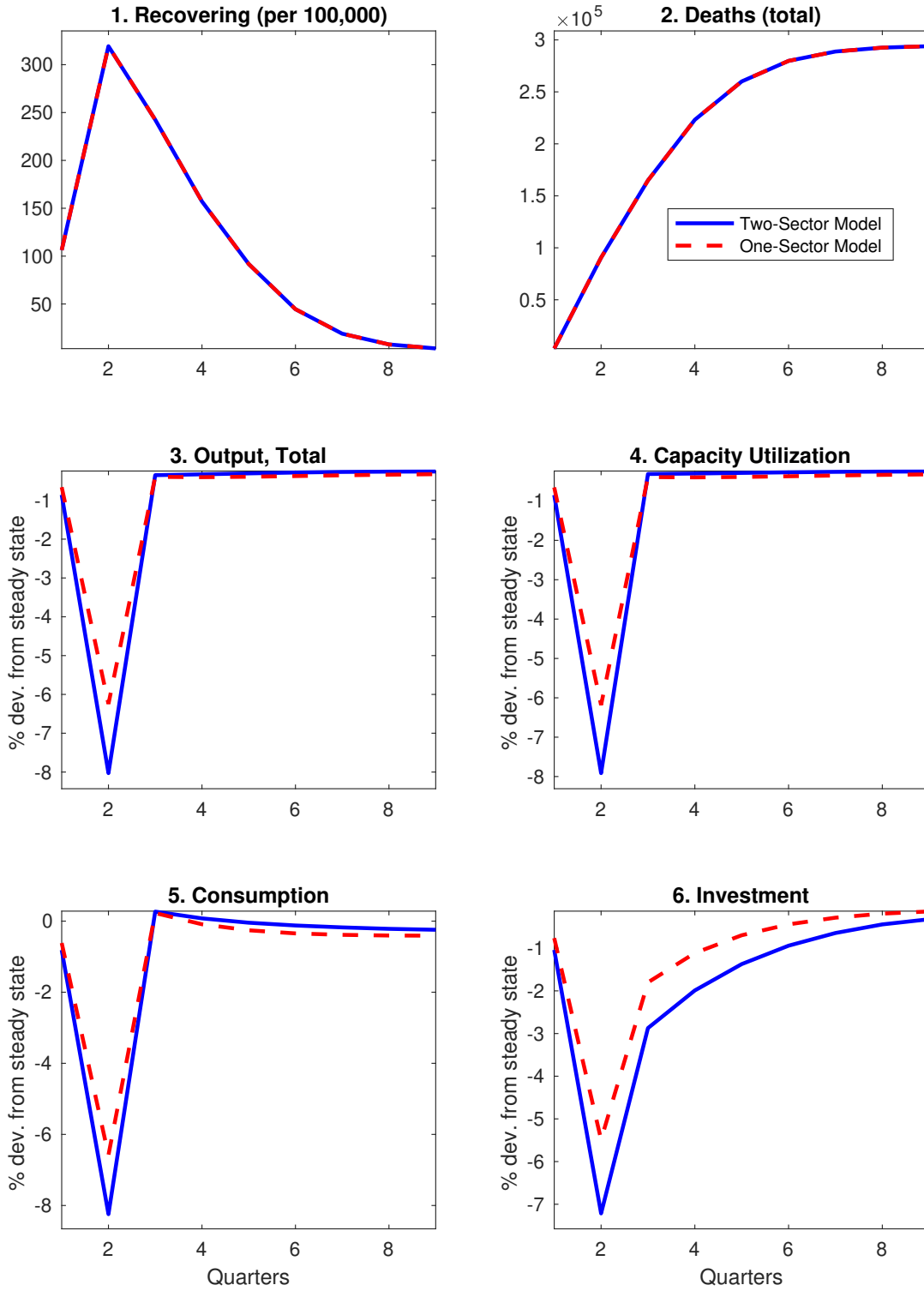
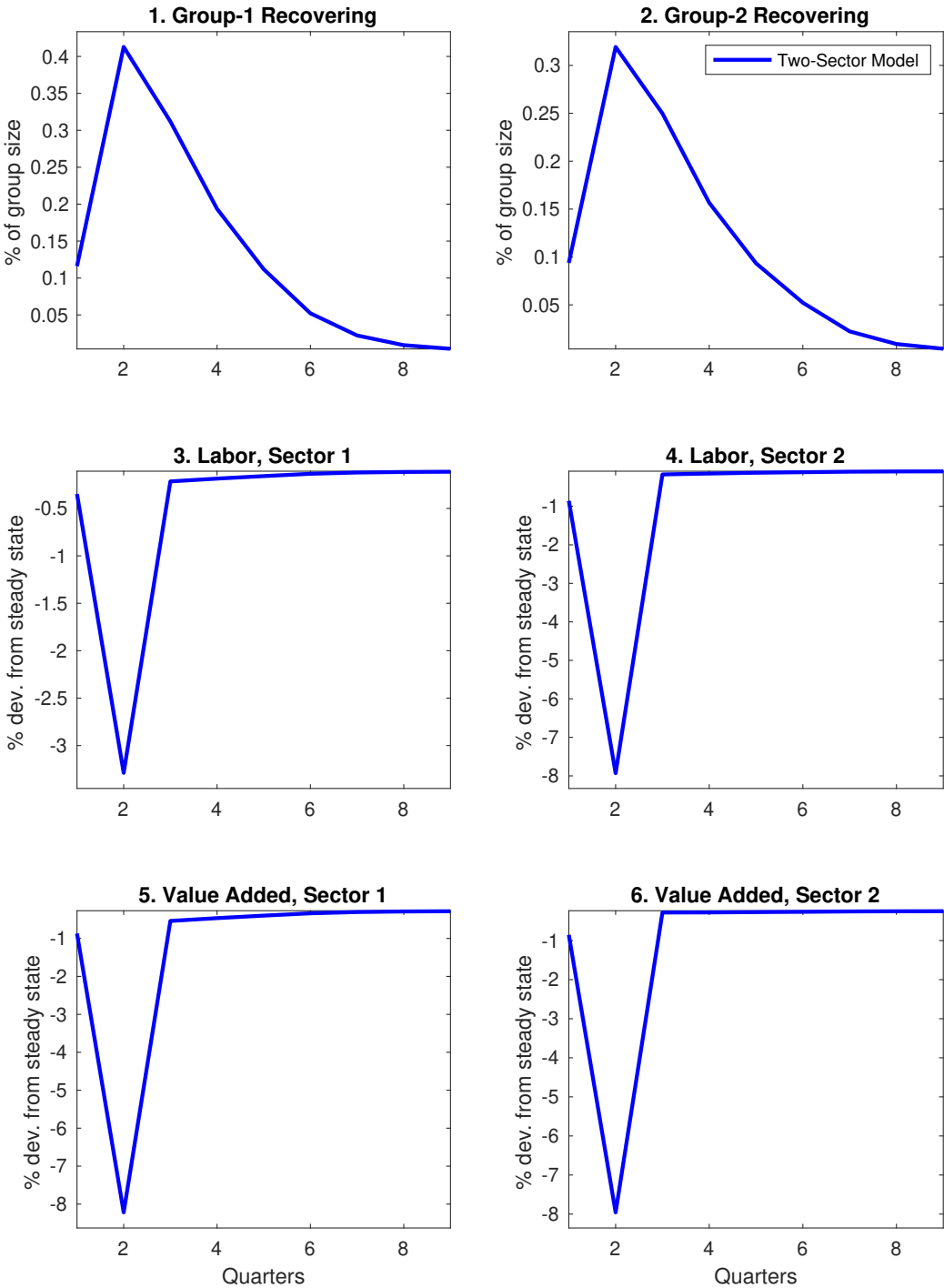


Figure 5: Economic Consequences of COVID-19: Sectoral Detail for the Two-Sector Model



Note: This figure provides additional sectoral details for the two-sector model, complementing the paths for aggregate variables shown in Figure 4.

Figure 6: Comparing the Aggregate Economic Consequences of COVID-19 with and Without Social Distancing: A Two-Sector Approach

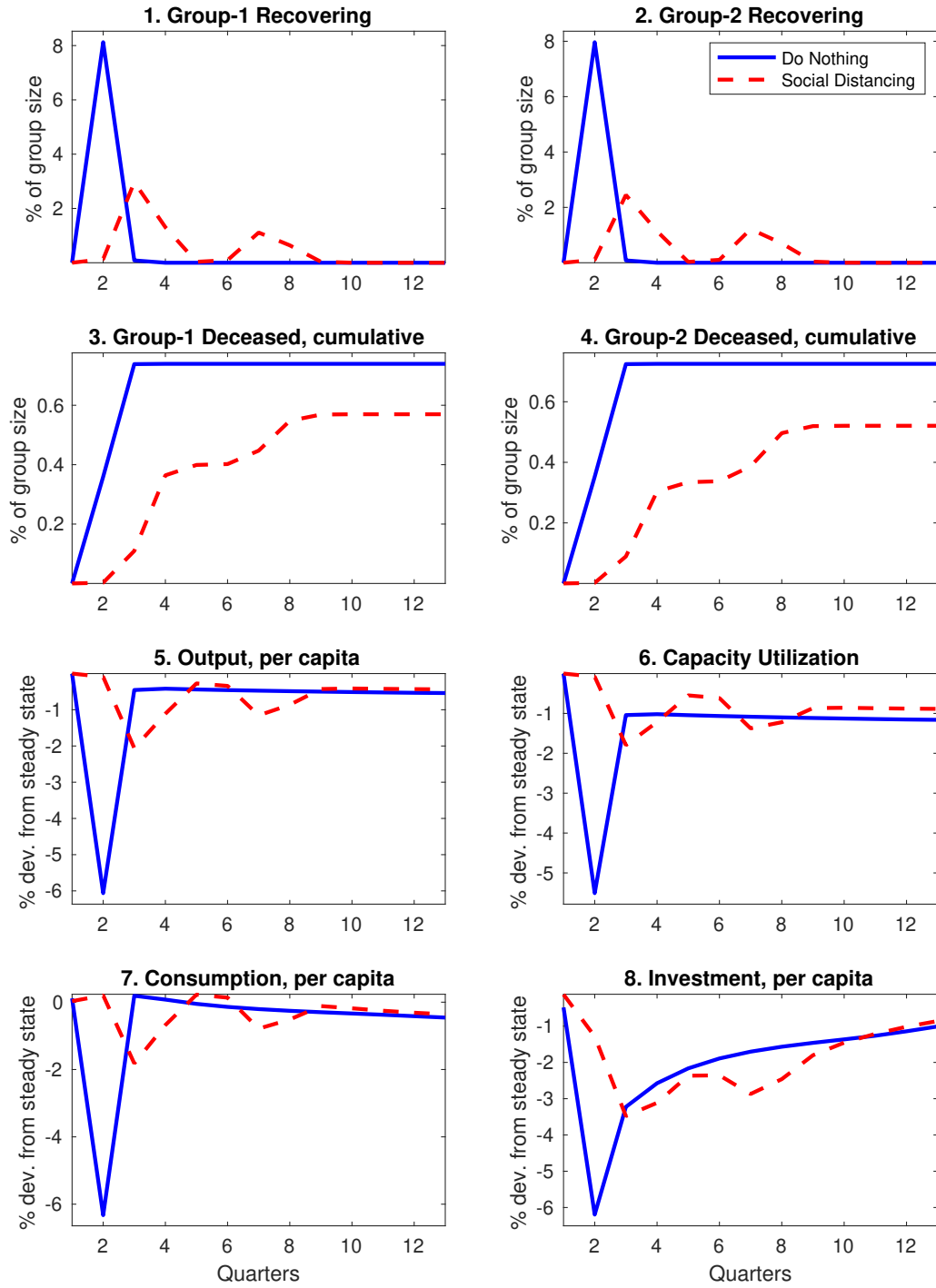
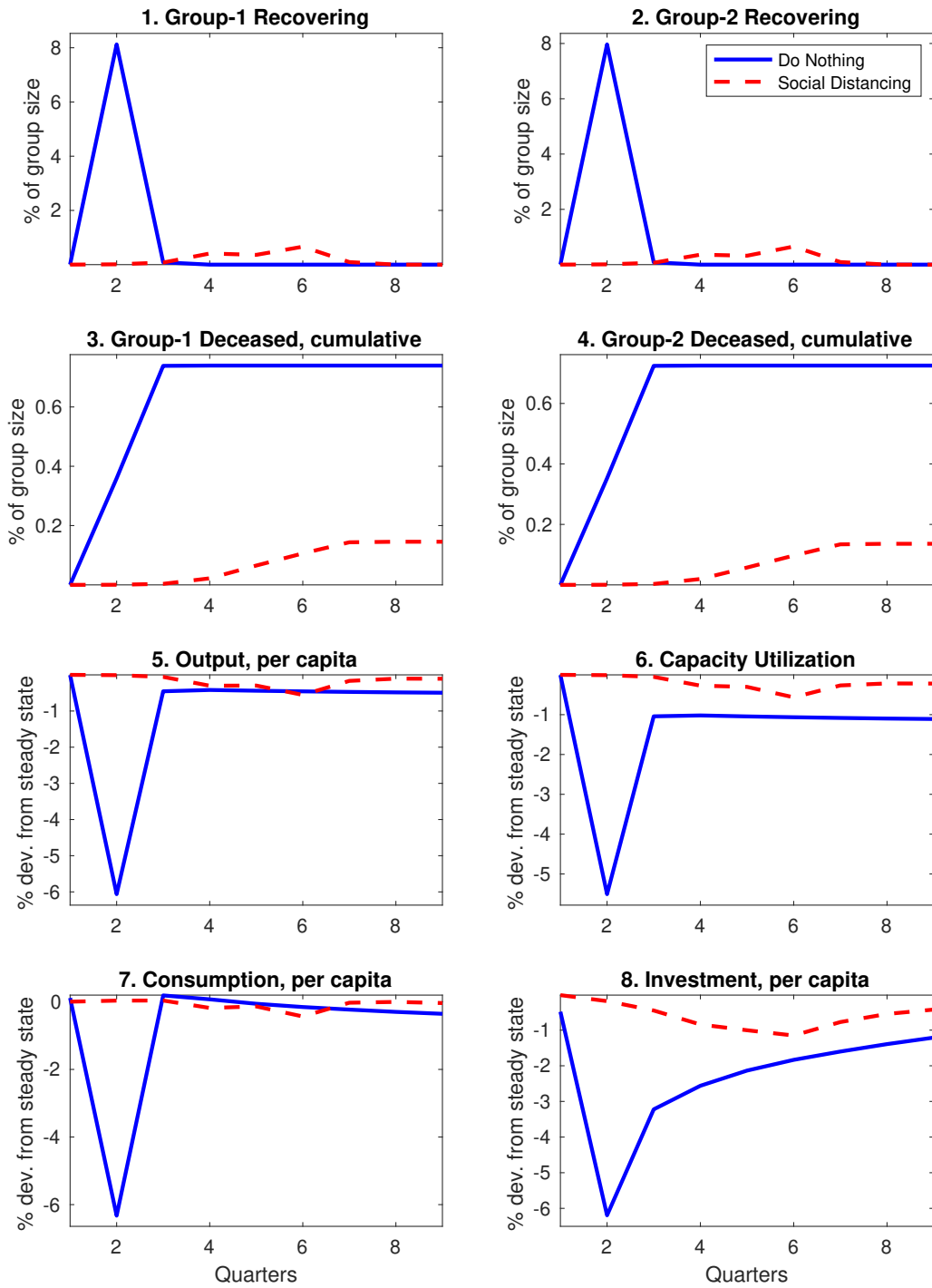


Figure 7: Waiting for a Vaccine



Online Appendix to “Social Distancing and Supply Disruptions in a Pandemic”

Martin Bodenstein Giancarlo Corsetti Luca Guerrieri
 Federal Reserve Board University of Cambridge Federal Reserve Board

A Additional Details for the Two-Sector Model

This appendix derives the equilibrium conditions for the two-sector model and the steady-state condition. Finally, it also shows the derivation of the elasticity of substitution between the two factor inputs in the production function for final output goods.

A.1 Equilibrium conditions

Households maximize

$$\begin{aligned} & \max_{c_t, \lambda_{c,t}, i_t, k_t, \lambda_{k,t}, u_t, \lambda_{i,t}} E_t \sum_{i=0}^{\infty} \beta^i [\log(c_{t+i} - \kappa c_{t+i-1}) \\ & + \lambda_{c,t+i} \left(-c_{t+i} - i_{t+i} + w_{1,t+i} l_{1,t+i} + w_{2,t+i} l_{2,t+i} + r_{k,t+i} u_t k_{t+i-1} - \nu_0 \frac{u_t^{1+\nu}}{1+\nu} - \frac{\zeta (i_t - i_{t-1})^2}{2 i_{t-1}} \right) \\ & + \lambda_{k,t+i} (-k_{t+i} + (1 - \delta) k_{t+i-1} + i_{t+i}) + \lambda_{i,t+i} (i_t - \phi i^{ss})]. \end{aligned}$$

These are the first-order conditions from the households' problem:

$$\frac{1}{c_t - \kappa c_{t-1}} - \beta \kappa E_t \frac{1}{c_{t+1} - \kappa c_t} = \lambda_{c,t}, \quad (30)$$

$$c_t + i_t = w_{1,t} l_{1,t} + w_{2,t} l_{2,t} + r_{k,t} k_{t-1} - \nu_0 \frac{u_t^{1+\nu}}{1+\nu} - \frac{\zeta (i_t - i_{t-1})^2}{2 i_{t-1}}, \quad (31)$$

$$\lambda_{c,t} \left[1 + \zeta \frac{(i_t - i_{t-1})}{i_{t-1}} \right] - \beta \lambda_{c,t+1} \left[\zeta \frac{(i_{t+1} - i_t)}{i_t} + \frac{\zeta (i_{t+1} - i_t)^2}{2 i_t^2} \right] = \lambda_{k,t} + \lambda_{i,t+i}, \quad (32)$$

$$E_t \lambda_{c,t+1} r_{k,t+1} u_{t+1} - \lambda_{k,t} + \beta (1 - \delta) E_t \lambda_{k,t+1} = 0, \quad (33)$$

$$k_t = (1 - \delta) k_{t-1} + i_t, \quad (34)$$

$$\lambda_{c,t} r_{k,t} k_{t-1} = \lambda_{c,t} \nu_0 u_t^\nu, \quad (35)$$

and the complementary slackness condition

$$\lambda_{i,t+i} (i_t - \phi i^{ss}) = 0. \quad (36)$$

Firms in Sector 1 solve this cost-minimization problem

$$\min_{l_t^1} w_t l_t^1 + p_t^1 [v^1 - \gamma (l_t^1 - \nu)]$$

And from the production function, we also have that

$$v_t^1 = \max [\gamma (l_t^1 - \chi), 0] \quad (37)$$

and that

$$w_t = \gamma p_t^1. \quad (38)$$

Firms in Sector 2 solve this cost-minimization problem

$$\begin{aligned} & \min_{u_t k_{t-1}, l_{2,t}^1, v_t^1} r_{k,t} u_t k_{t-1} + w_{2,t} l_{2,t} + p_{1,t} v_{1,t} \\ & + \left[y_t - \left((1 - \omega)^{\frac{\rho}{1+\rho}} (v_{1,t})^{\frac{1}{1+\rho}} + \omega^{\frac{\rho}{1+\rho}} \left((u_t k_{t-1})^\alpha (l_{2,t})^{1-\alpha} \right)^{\frac{1}{1+\rho}} \right)^{1+\rho} \right] \end{aligned}$$

Notice that firms choose $u_t k_{t-1}$ as if it were a single input, representing capital services. The first-order conditions for this problem are:

$$\begin{aligned} r_{k,t} - (1 + \rho) \left((1 - \omega)^{\frac{\rho}{1+\rho}} (v_{1,t})^{\frac{1}{1+\rho}} + \omega^{\frac{\rho}{1+\rho}} \left(k_{t-1}^\alpha l_{2,t}^{1-\alpha} \right)^{\frac{1}{1+\rho}} \right)^\rho \\ \frac{1}{1+\rho} \omega^{\frac{\rho}{1+\rho}} \left((u_t k_{t-1})^\alpha l_{2,t}^{1-\alpha} \right)^{\frac{1}{1+\rho}-1} \alpha (u_t k_{t-1})^{\alpha-1} l_{2,t}^{1-\alpha} = 0. \end{aligned}$$

Notice that $y^x = \left((1 - \omega)^{\frac{\rho}{1+\rho}} (v_{1,t})^{\frac{1}{1+\rho}} + \omega^{\frac{\rho}{1+\rho}} \left((u_t k_{t-1})^\alpha (l_{2,t})^{1-\alpha} \right)^{\frac{1}{1+\rho}} \right)^{(1+\rho)x}$. Find x , such that $x(1 + \rho) = \rho$. That is $x = \frac{\rho}{1+\rho}$. Accordingly,

$$r_{k,t} - y^{\frac{\rho}{1+\rho}} \omega^{\frac{\rho}{1+\rho}} (v_{2,t})^{-\frac{\rho}{1+\rho}} \alpha \frac{v_{2,t}}{u_t k_{t-1}} = 0.$$

Which can be further simplified as

$$r_{k,t} = \alpha \left(\omega \frac{y_t}{v_{2,t}} \right)^{\frac{\rho}{1+\rho}} \frac{v_{2,t}}{u_t k_{t-1}}. \quad (39)$$

$$w_{2,t} = (1 - \alpha) \left(\omega \frac{y_t}{v_{2,t}} \right)^{\frac{\rho}{1+\rho}} \frac{v_{2,t}}{l_{2,t}}. \quad (40)$$

$$p_{1,t} - (1 + \rho) \left((1 - \omega)^{\frac{\rho}{1+\rho}} (v_{1,t})^{\frac{1}{1+\rho}} + \omega^{\frac{\rho}{1+\rho}} \left((u_t k_{t-1})^\alpha (l_{2,t})^{1-\alpha} \right)^{\frac{1}{1+\rho}} \right)^\rho \frac{1}{1 + \rho} (1 - \omega)^{\frac{\rho}{1+\rho}} (v_{1,t})^{\frac{1}{1+\rho}-1} = 0.$$

Simplifying

$$p_{1,t} - y^{\frac{\rho}{1+\rho}} (1 - \omega)^{\frac{\rho}{1+\rho}} (v_{1,t})^{-\frac{\rho}{1+\rho}} = 0.$$

$$p_{1,t} = \left(\frac{(1 - \omega) y}{v_{1,t}} \right)^{\frac{\rho}{1+\rho}}. \quad (41)$$

And from the production function,

$$y_t = \left((1 - \omega)^{\frac{\rho}{1+\rho}} (v_{1,t})^{\frac{1}{1+\rho}} + \omega^{\frac{\rho}{1+\rho}} (v_{2,t})^{\frac{1}{1+\rho}} \right)^{1+\rho} \quad (42)$$

and where

$$v_{2,t} = (u_t k_{t-1})^\alpha (l_{2,t})^{1-\alpha}. \quad (43)$$

And from the budget constraint we can derive that the goods market must clear

$$y_t = c_t + i_t + \nu_0 \frac{u_t^{1+\nu}}{1+\nu} + \frac{\zeta}{2} \frac{(i_t - i_{t-1})^2}{i_{t-1}}.$$

The 14 equations above allow us to determine 14 variables $y_t, v_{1,t}, v_{2,t}, c_t, i_t, k_t, u_t, \lambda_{c,t}, \lambda_{i,t}, \lambda_{k,t}, p_{1,t}, w_{1,t}, w_{2,t}, r_{k,t}$, with $l_{1,t}$ and $l_{2,t}$ determined by exogenous processes.

A.2 Steady-State Conditions

Set $u_t = 1$ and later set ν_0 to support this choice. Notice that the investment constraint must be slack in the steady state, so

$$\lambda_i = 0. \quad (44)$$

Using

$$\lambda_{c,t} = \lambda_{k,t} + \lambda_{i,t},$$

and $\lambda_{c,t} r_{k,t} - \lambda_{k,t} + \theta(1 - \delta) E_t \lambda_{i,t+1} = 0$, we can see that

$$r_k = 1 - \theta(1 - \delta). \quad (45)$$

Using

$$r_k = \alpha \left(\omega \frac{y}{v_2} \right)^{\frac{\rho}{1+\rho}} \frac{v_2}{k} \quad (46)$$

and combining it with $r_k = 1 - \theta(1 - \delta)$, we can use a numerical solver to get k , given l_1 and l_2 .

Knowing k , and with

$$v_1 = \eta(l_1 - \chi), \quad (47)$$

we can solve for y using the production function

$$y = \left((1 - \omega)^{\frac{\rho}{1+\rho}} (v_1)^{\frac{1}{1+\rho}} + \omega^{\frac{\rho}{1+\rho}} (k^\alpha (l_2)^{1-\alpha})^{\frac{1}{1+\rho}} \right)^{1+\rho} \quad (48)$$

From $k_t = (1 - \delta)k_{t-1} + i_t$, we have that

$$i = \delta k \quad (49)$$

Using $\lambda_{c,t} r_{k,t} k_{t-1} = \lambda_{c,t} \nu_0 u_t^\nu$, find the value of ν_0 that ensures $u = 1$. Accordingly

$$\nu_0 = r_k k \quad (50)$$

And using the resource constraint, we can solve for c

$$c = y - i - \nu_0 \frac{u_t^{1+\nu}}{1+\nu} \quad (51)$$

$$\lambda_c = \frac{1}{(1-\kappa)c} - \theta\kappa \frac{1}{(1-\kappa)c}. \quad (52)$$

$$\lambda_k = \lambda_c \quad (53)$$

$$p_1 = \left(\frac{(1-\omega)y}{l_1} \right)^{\frac{\rho}{1+\rho}} \quad (54)$$

$$w_1 = \eta p_1 \quad (55)$$

$$v_2 = k^\alpha (l_2)^{1-\alpha} \quad (56)$$

$$w_2 = (1-\alpha) \left(\omega \frac{y}{v_2} \right)^{\frac{\rho}{1+\rho}} \frac{v_2}{l_2} \quad (57)$$

A.3 Deriving the Elasticity of Substitution for the Production Function of Sector 2

$$y_t = \left((1-\omega)^{\frac{\rho}{1+\rho}} (v_{1,t})^{\frac{1}{1+\rho}} + \omega^{\frac{\rho}{1+\rho}} (v_{2,t})^{\frac{1}{1+\rho}} \right)^{1+\rho}$$

$$\frac{\partial y_t}{\partial v_{1,t}} = (1+\rho) \left((1-\omega)^{\frac{\rho}{1+\rho}} (\eta(l_{1,t} - \nu))^{\frac{1}{1+\rho}} + \omega^{\frac{\rho}{1+\rho}} (v_{2,t})^{\frac{1}{1+\rho}} \right)^\rho \frac{1}{1+\rho} (1-\omega)^{\frac{\rho}{1+\rho}} (v_{1,t})^{\frac{1}{1+\rho}-1}$$

Notice again that $y^x = \left((1-\omega)^{\frac{\rho}{1+\rho}} (\eta(l_{1,t} - \nu))^{\frac{1}{1+\rho}} + \omega^{\frac{\rho}{1+\rho}} (v_{2,t})^{\frac{1}{1+\rho}} \right)^{(1+\rho)x}$. Find x , such that $x(1+\rho) = \rho$. That is $x = \frac{\rho}{1+\rho}$. Accordingly,

$$\frac{\partial y_t}{\partial v_{1,t}} = y^{\frac{\rho}{1+\rho}} (1-\omega)^{\frac{\rho}{1+\rho}} \eta (v_{1,t})^{-\frac{\rho}{1+\rho}}$$

$$\frac{\partial y_t}{\partial v_{2,t}} = y^{\frac{\rho}{1+\rho}} (\omega)^{\frac{\rho}{1+\rho}} (v_{2,t})^{-\frac{\rho}{1+\rho}}$$

$$\frac{\frac{\partial y_t}{\partial v_{1,t}}}{\frac{\partial y_t}{\partial v_{2,t}}} = \frac{(1-\omega)^{\frac{\rho}{1+\rho}} (v_{1,t})^{-\frac{\rho}{1+\rho}}}{(\omega)^{\frac{\rho}{1+\rho}} (v_{2,t})^{-\frac{\rho}{1+\rho}}}$$

$$\log \frac{\frac{\partial y_t}{\partial v_{1,t}}}{\frac{\partial y_t}{\partial v_{2,t}}} = \log \left(\frac{(1-\omega)^{\frac{\rho}{1+\rho}} (v_{1,t})^{-\frac{\rho}{1+\rho}}}{(\omega)^{\frac{\rho}{1+\rho}} (v_{2,t})^{-\frac{\rho}{1+\rho}}} \right) = \log \left(\frac{(1-\omega)^{\frac{\rho}{1+\rho}}}{(\omega)^{\frac{\rho}{1+\rho}}} \right) + \frac{\rho}{1+\rho} \log \frac{v_{2,t}}{v_{1,t}}$$

The elasticity is given by

$$Elast = \frac{d \log(v_{2,t}/v_{1,t})}{d \log(\frac{\partial y_t}{\partial v_{1,t}}/\frac{\partial y_t}{\partial v_{2,t}})} = \frac{1+\rho}{\rho}$$

Therefore to hit a destired elasticity set ρ as

$$\rho Elast - \rho = 1$$

$$\rho = \frac{1}{Elast - 1}.$$

B Calibration of the Minimum-Scale Parameter and Additional Sensitivity Analysis

To calibrate the minimum-scale parameter for the production function of Sector 1 in the two-sector model, see Equation 22, we adopt the following strategy. We feed into the model a path of labor supply shocks that meets two restrictions: 1) it balances the decline in value added across sectors and 2) it brings about a reduction in labor inputs in line with the increase in the unemployment rate relative to the 3.5 percent mark observed in February, 2020. We then set the minimum scale parameter to match a 12 percent decline in GDP in the the second quarter of 2020. We calculated this decline relative to the consensus level of GDP in the Blue Chip forecasts published in January 2020, before private forecasters entertained the possibility of a pandemic. The resulting calibration choice for the parameter χ is $\frac{6}{10}$ times the steady state value for the labor input of Sector 1.

Figure A.1 compares one- and two-sector models that match the observed increase in unemployment from March through October 2020 relative to the level in February 2020. After October 2020, the labor supply shocks follow an auto-regressive process with a coefficient of 0.95. The figure shows sizable differences between the economic collapse that can be matched with our two-sector model and the smaller economic decline implied by the special case of a one-sector model. We conclude that our two-sector model is a more appropriate choice to study the economic consequences of the COVID-19 pandemic.

B.1 Sensitivity Analysis

Figure A.2 offers sensitivity analysis pertaining to the comparison on the economic effects of the spread of COVID-19 without any social distancing measures. We compare the economic effects using one- and two-sector models. Figure A.2 considers sensitivity to a range of values of the initial reproduction rate. It shows that the differences between the one- and two-sector models persist as long as the reproduction rate does not drop below 1.2, a level that would also curtail the spread of the disease.

Figures A.3 and A.4 complement the discussion of the cost of waiting for a vaccine in Section 5.3. They pertain, respectively, to sensitivity analysis to the effectiveness of the lockdown and to the probability of transmission of the disease for given contacts.

Figure A.1: Using the Two-Sector Model to Match the Observed Increase in the Unemployment Rate Relative to February 2020

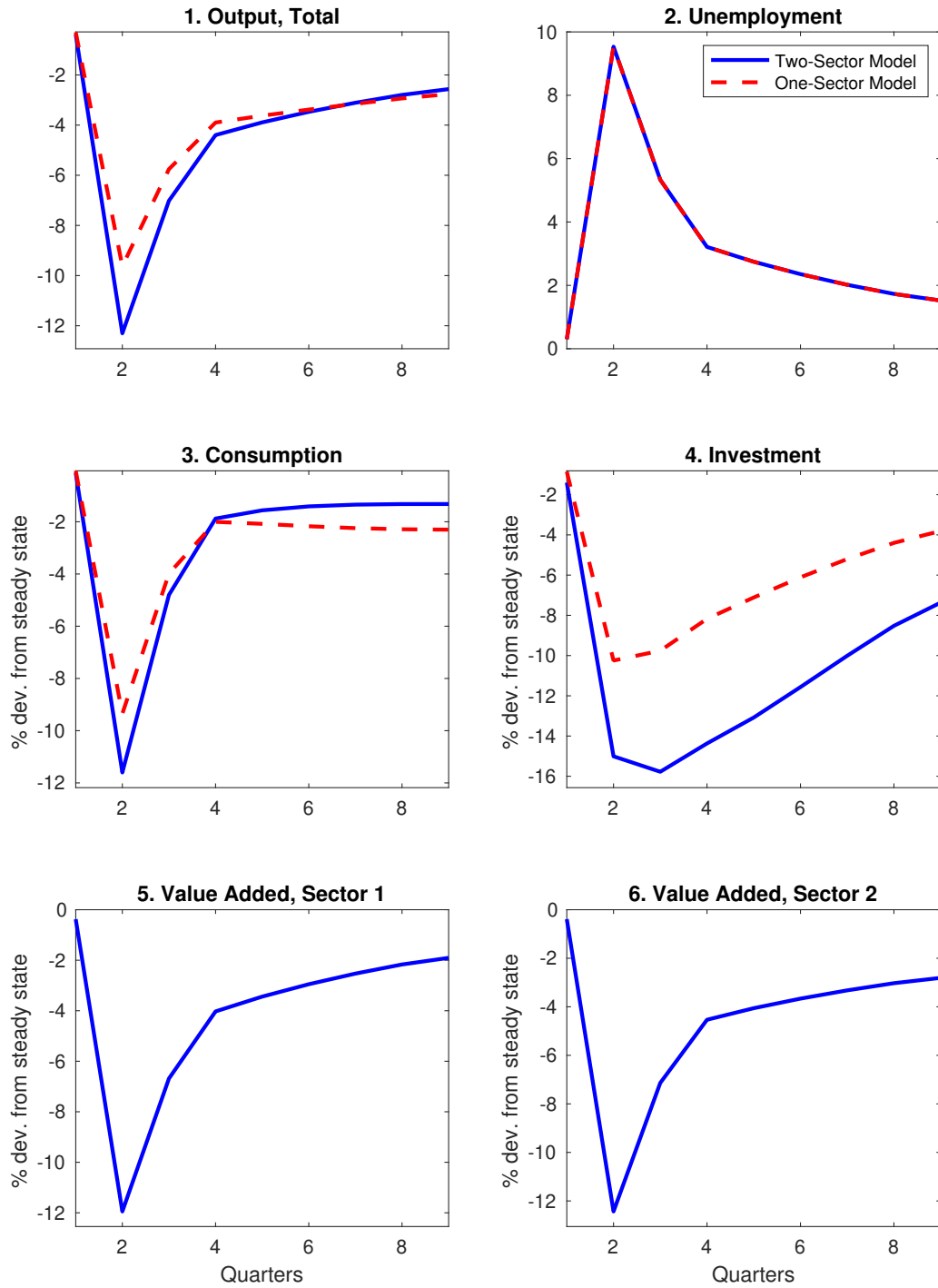
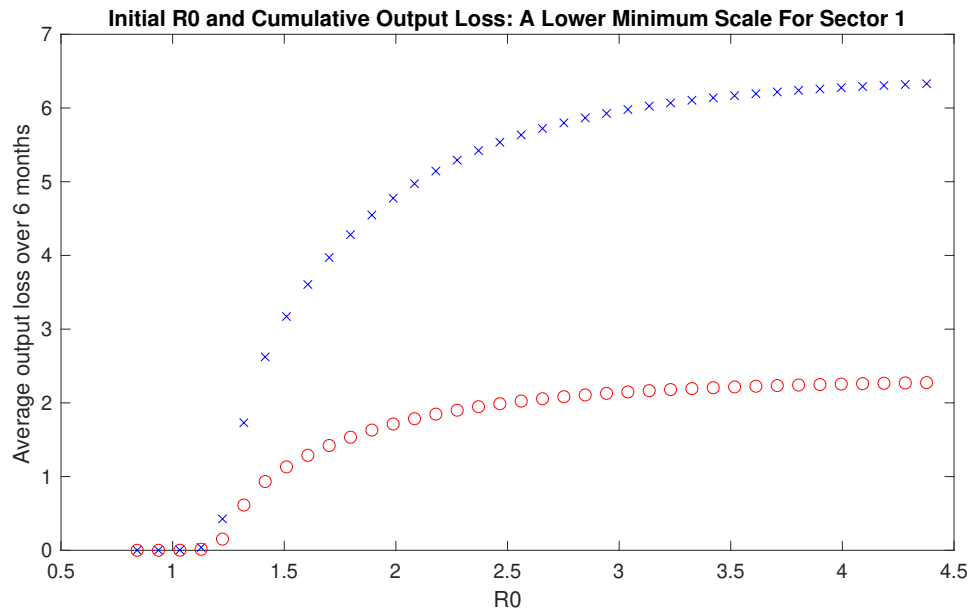
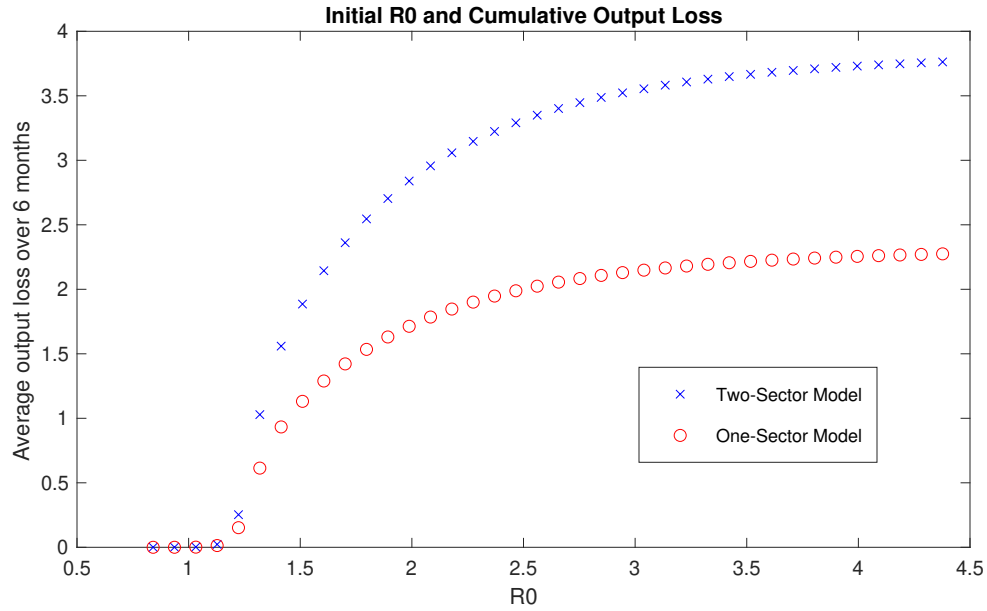


Figure A.2: Comparing the Aggregate Economic Consequences of COVID-19 Without Social Distancing in One- and Two-Sector Models: Sensitivity to the Reproduction Rate



Note: We assume that no social distancing measures are taken to reduce the spread of the disease. The output loss stems from the reduction in labor supply from symptomatic infected individuals. The figure shows the cumulative output loss over six months alternatively based on one- and two-sector models for different values of the reproduction rate (set to 2 in our baseline). The top panel keeps all other parameters at their baseline values. For the bottom panel, we have increased the minimum scale parameter for Sector 1, χ , to $\frac{8}{10}$ of the steady state labor input, as opposed to $\frac{6}{10}$ in the baseline calibration.

Figure A.3: Waiting for a Vaccine: A Lower Effectiveness of the Lockdown at Reducing Contact Rates

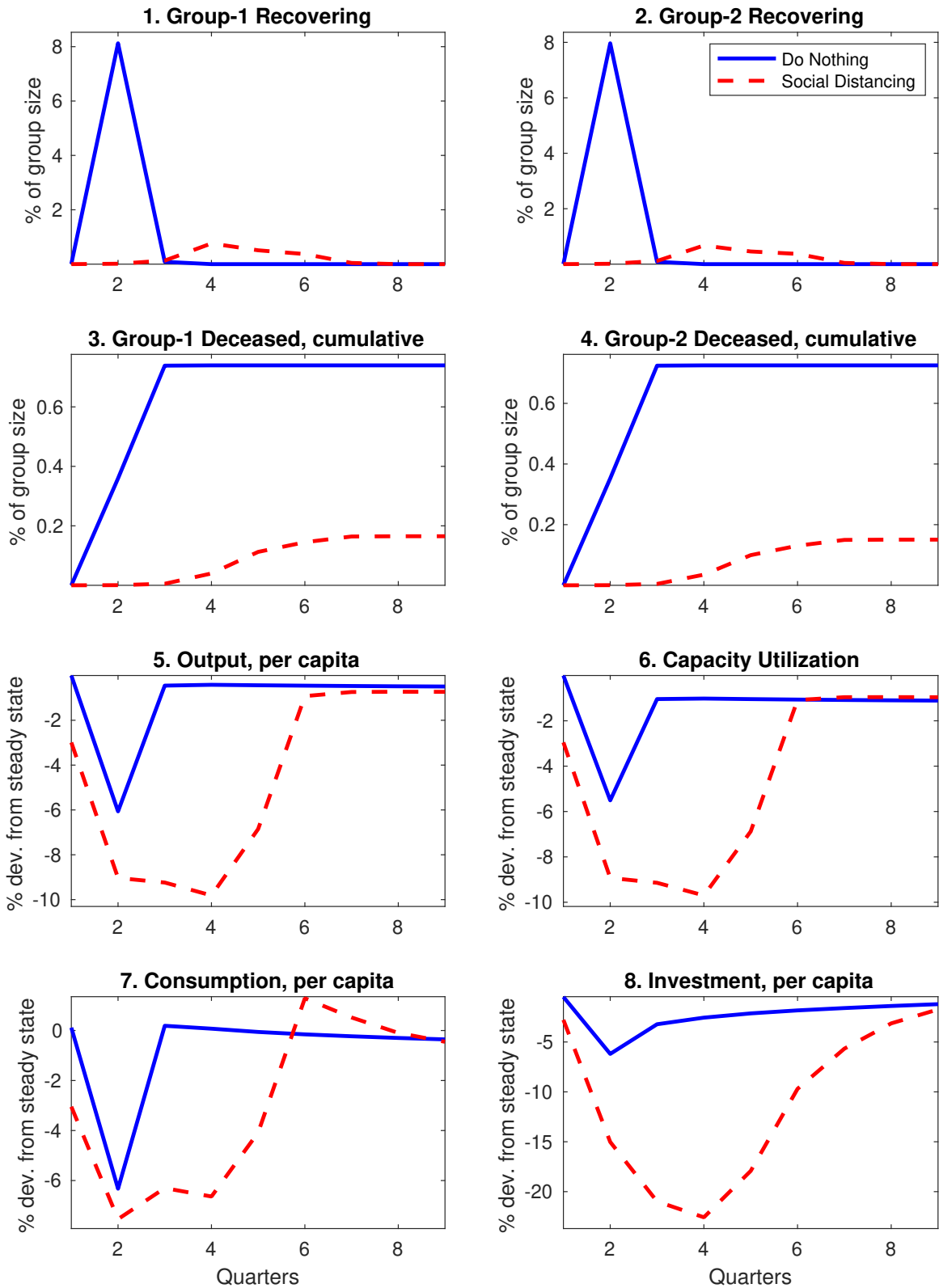


Figure A.4: Waiting for a Vaccine: A 70 Percent Increase in the Transmissibility of the Virus

